

Formal Methods for Event Processing

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Tutorial Resources

- ▶ Alexander Artikis, Anastasios Skarlatidis, Francois Portet, Georgios Paliouras: Logic-based event recognition. Knowledge Engineering Review 27(4): 469-506 (2012).
- ▶ Software, datasets, slides & papers at cer.iit.demokritos.gr

Event Recognition (Event Pattern Matching)

Input:

- ▶ Symbolic representation of time-stamped, **low-level events (LLE)** coming from (geographically distributed) sources.
- ▶ Big Data.

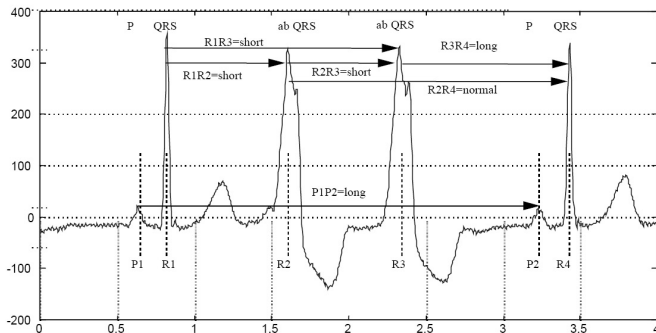
Output:

- ▶ **High-level events (HLE)** — collections of LLE and/or HLE that satisfy some pattern (temporal, spatial, logical constraints).
 - ▶ Not restricted to aggregates.
- ▶ Humans understand HLE easier than LLE.

Tutorial scope:

- ▶ Systems with a **formal semantics**.

Cardiac Arrhythmia Recognition



- ▶ **LLE:** P and QRS waves representing heart activity.
- ▶ **HLE:** Cardiac arrhythmias.

A cardiac arrhythmia is defined as a **temporal** combination of P and QRS waves.

Cardiac Arrhythmia Recognition

Input	Output
16338 qrs[normal]	
17091 p_wave[normal]	
17250 qrs[normal]	
17952 p_wave[normal]	
18913 p_wave[normal]	
19066 qrs[normal]	
19838 p_wave[normal]	
20713 p_wave[normal]	
20866 qrs[normal]	
21413 qrs[abnormal]	
21926 p_wave[normal]	
22496 qrs[normal]	
...	

Cardiac Arrhythmia Recognition

Input	Output
16338 qrs[normal]	[17091, 19066] mobitzII
17091 p_wave[normal]	
17250 qrs[normal]	
17952 p_wave[normal]	
18913 p_wave[normal]	
19066 qrs[normal]	
19838 p_wave[normal]	
20713 p_wave[normal]	
20866 qrs[normal]	
21413 qrs[abnormal]	
21926 p_wave[normal]	
22496 qrs[normal]	
...	

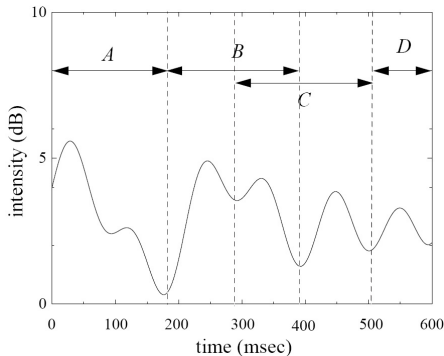
Cardiac Arrhythmia Recognition

Input	Output
77091 qrs[normal]	
77250 p_wave[normal]	
77952 qrs[normal]	
78913 qrs[abnormal]	
79066 p_wave[normal]	
79838 qrs[normal]	
80000 qrs[abnormal]	
80713 p_wave[normal]	
80866 qrs[normal]	
81413 qrs[abnormal]	
81926 p_wave[normal]	
...	

Cardiac Arrhythmia Recognition

Input	Output
77091 qrs[normal]	[78913, 81413] bigeminy
77250 p_wave[normal]	
77952 qrs[normal]	
78913 qrs[abnormal]	
79066 p_wave[normal]	
79838 qrs[normal]	
80000 qrs[abnormal]	
80713 p_wave[normal]	
80866 qrs[normal]	
81413 qrs[abnormal]	
81926 p_wave[normal]	
...	

Humpback Whale Song Recognition



- ▶ **LLE**: Song units representing whale sounds.
- ▶ **HLE**: Whale songs.

A whale song is defined as a **temporal** combination of songs units.

Humpback Whale Song Recognition

Input	Output
[200, 400]	A
[400, 500]	B
[500, 550]	C
[600, 700]	B
[700, 800]	D
[800, 1000]	A
[1050, 1200]	E
[1300, 1500]	B
[1600, 1800]	E
[1800, 1900]	C
[1900, 2000]	B
...	

Humpback Whale Song Recognition

Input		Output	
[200, 400]	A	[200, 550]	S_1
[400, 500]	B	[700, 1200]	S_2
[500, 550]	C	[1600, 2000]	S_3
[600, 700]	B	...	
[700, 800]	D		
[800, 1000]	A		
[1050, 1200]	E		
[1300, 1500]	B		
[1600, 1800]	E		
[1800, 1900]	C		
[1900, 2000]	B		
...			

Event Recognition for Maritime Surveillance

LLE:

- ▶ Vessel movement.
- ▶ Entering/leaving port.
- ▶ Communication gap.

HLE:

- ▶ Shipping in protected areas.
- ▶ Shipping in unsafe areas.
- ▶ Loitering.
- ▶ Collision.
- ▶ Forbidden fishing.

HLE are **spatio-temporal** combinations of LLE and **background knowledge**.

Event Recognition for Energy Management

Houses



Sensors



Data Fusion



Event Recognition



Action



LLE:

- ▶ Credit card transactions from all over the world.

HLE:

- ▶ Cloned card — a credit card is being used simultaneously in different countries.
- ▶ Spike usage — the 24-hour running sum is considerably higher than the monthly average of the last 6 months.
- ▶ New high use — the card is being frequently used in merchants or countries never used before.
- ▶ Potential batch fraud — many transactions from multiple cards in the same point-of-sale terminal in high amounts.

A fraud is a **spatio-temporal** combination of transactions and **background knowledge**.

Running Example I: Event Recognition for Public Space Surveillance

**SURVEILLANCE
CAMERAS**



**SHORT-TERM
ACTIVITY
RECOGNITION**



**LONG-TERM
ACTIVITY
RECOGNITION**



**HUMAN
OPERATOR**



Event Recognition for Public Space Surveillance

Input	Output
340 <i>inactive</i> (id_0)	
340 $p(id_0) = (20.88, -11.90)$	
340 <i>appear</i> (id_0)	
340 <i>walking</i> (id_2)	
340 $p(id_2) = (25.88, -19.80)$	
340 <i>active</i> (id_1)	
340 $p(id_1) = (20.88, -11.90)$	
340 <i>walking</i> (id_3)	
340 $p(id_3) = (24.78, -18.77)$	
380 <i>walking</i> (id_3)	
380 $p(id_3) = (27.88, -9.90)$	
380 <i>walking</i> (id_2)	
380 $p(id_2) = (28.27, -9.66)$	

Event Recognition for Public Space Surveillance

Input	Output
340 <i>inactive</i> (id_0)	340 <i>leaving_object</i> (id_1, id_0)
340 $p(id_0) = (20.88, -11.90)$	
340 <i>appear</i> (id_0)	
340 <i>walking</i> (id_2)	
340 $p(id_2) = (25.88, -19.80)$	
340 <i>active</i> (id_1)	
340 $p(id_1) = (20.88, -11.90)$	
340 <i>walking</i> (id_3)	
340 $p(id_3) = (24.78, -18.77)$	
380 <i>walking</i> (id_3)	
380 $p(id_3) = (27.88, -9.90)$	
380 <i>walking</i> (id_2)	
380 $p(id_2) = (28.27, -9.66)$	

Event Recognition for Public Space Surveillance

Input	Output
340 <i>inactive</i> (id_0)	340 <i>leaving_object</i> (id_1, id_0)
340 $p(id_0) = (20.88, -11.90)$	<i>since</i> (340) <i>moving</i> (id_2, id_3)
340 <i>appear</i> (id_0)	
340 <i>walking</i> (id_2)	
340 $p(id_2) = (25.88, -19.80)$	
340 <i>active</i> (id_1)	
340 $p(id_1) = (20.88, -11.90)$	
340 <i>walking</i> (id_3)	
340 $p(id_3) = (24.78, -18.77)$	
380 <i>walking</i> (id_3)	
380 $p(id_3) = (27.88, -9.90)$	
380 <i>walking</i> (id_2)	
380 $p(id_2) = (28.27, -9.66)$	

Event Recognition for Public Space Surveillance

Input	Output
420 <i>active</i> (id_4)	
420 $p(id_4) = (10.88, -71.90)$	
420 <i>inactive</i> (id_3)	
420 $p(id_3) = (5.8, -50.90)$	
420 <i>abrupt</i> (id_5)	
420 $p(id_5) = (11.80, -72.80)$	
420 <i>active</i> (id_6)	
420 $p(id_6) = (7.8, -52.90)$	
480 <i>abrupt</i> (id_4)	
480 $p(id_4) = (20.45, -12.90)$	
480 <i>abrupt</i> (id_5)	
480 $p(id_5) = (17.88, -11.90)$	
...	

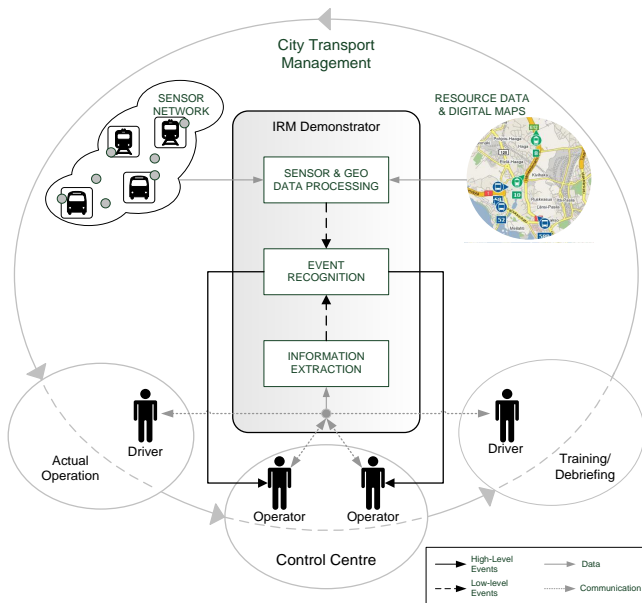
Event Recognition for Public Space Surveillance

Input	Output
420 <i>active</i> (id_4)	[420, 480] <i>fighting</i> (id_4, id_5)
420 $p(id_4) = (10.88, -71.90)$	
420 <i>inactive</i> (id_3)	
420 $p(id_3) = (5.8, -50.90)$	
420 <i>abrupt</i> (id_5)	
420 $p(id_5) = (11.80, -72.80)$	
420 <i>active</i> (id_6)	
420 $p(id_6) = (7.8, -52.90)$	
480 <i>abrupt</i> (id_4)	
480 $p(id_4) = (20.45, -12.90)$	
480 <i>abrupt</i> (id_5)	
480 $p(id_5) = (17.88, -11.90)$	
...	

Event Recognition for Public Space Surveillance

Input	Output
420 <i>active</i> (id_4)	[420, 480] <i>fighting</i> (id_4, id_5)
420 $p(id_4) = (10.88, -71.90)$	<i>since</i> (420) <i>meeting</i> (id_3, id_6)
420 <i>inactive</i> (id_3)	
420 $p(id_3) = (5.8, -50.90)$	
420 <i>abrupt</i> (id_5)	
420 $p(id_5) = (11.80, -72.80)$	
420 <i>active</i> (id_6)	
420 $p(id_6) = (7.8, -52.90)$	
480 <i>abrupt</i> (id_4)	
480 $p(id_4) = (20.45, -12.90)$	
480 <i>abrupt</i> (id_5)	
480 $p(id_5) = (17.88, -11.90)$	
...	

Running Example II



Event Recognition for Transport & Traffic Management

	Input	Output
200	scheduled stop enter	
215	late stop leave	
[215, 400]	abrupt acceleration	
[350, 600]	sharp turn	
620	<u>flow=low</u>	
	<u>density=high</u>	
700	scheduled stop enter	
720	<u>flow=low</u>	
	<u>density=average</u>	
820	scheduled stop leave	
...		

Event Recognition for Transport & Traffic Management

	Input	Output
200	scheduled stop enter	
215	late stop leave	<i>since(215)</i> non-punctual
[215, 400]	abrupt acceleration	
[350, 600]	sharp turn	[215, 600] uncomfortable driving
620	<u>flow=low</u>	
	<u>density=high</u>	<i>since(620)</i> congestion
700	scheduled stop enter	
720	<u>flow=low</u>	
	<u>density=average</u>	
820	scheduled stop leave	
...		

Event Recognition for Transport & Traffic Management

	Input	Output
200	scheduled stop enter	
215	late stop leave	<i>since(215)</i> non-punctual
[215, 400]	abrupt acceleration	
[350, 600]	sharp turn	[215, 600] uncomfortable driving
620	<u>flow=low</u>	
	<u>density=high</u>	<i>since(620)</i> congestion
700	scheduled stop enter	
720	<u>flow=low</u>	
	<u>density=average</u>	[620, 720] congestion
820	scheduled stop leave	[215, 820] non-punctual
...		

Event Recognition

Requirements:

- ▶ Efficient reasoning
 - ▶ to support real-time decision-making in large-scale, (geographically) distributed applications.
- ▶ Reasoning under uncertainty
 - ▶ to deal with various types of noise.
- ▶ Automated knowledge construction
 - ▶ to avoid the time-consuming, error-prone manual HLE definition development.

Tutorial Structure

- ▶ Temporal reasoning systems.
- ▶ Event recognition under uncertainty.
- ▶ Machine learning for event recognition.
- ▶ Open issues.

Tutorial Structure

- ▶ Temporal reasoning systems.
- ▶ Event recognition under uncertainty.
- ▶ Machine learning for event recognition.
- ▶ Open issues.

HLE Definition



HLE as Chronicle

A HLE can be defined as a set of events interlinked by time constraints and whose occurrence may depend on the context.

- ▶ This is the definition of a chronicle.

Chronicle recognition systems have been used in many applications:

- ▶ Cardiac monitoring system.
- ▶ Intrusion detection in computer networks.
- ▶ Distributed diagnosis of web services.

Chronicle Representation Language

Predicate	Meaning
<code>event(E, T)</code>	Event E takes place at time T
<code>event(F: (?V1, ?V2), T)</code>	An event takes place at time T changing the value of property F from ?V1 to ?V2
<code>noevent(E, (T1, T2))</code>	Event E does not take place between [T1, T2)
<code>noevent(F: (?V1, ?V2), (T1, T2))</code>	No event takes place between [T1, T2) that changes the value of property F from ?V1 to ?V2
<code>hold(F: ?V, (T1, T2))</code>	The value of property F is ?V between [T1, T2)
<code>occurs(N, M, E, (T1, T2))</code>	Event E takes place at least N times and at most M times between [T1, T2)

Chronicle Representation Language

```
chronicle punctual[?id, ?vehicle](T1) {  
  event( stop_enter[?id, ?vehicle, ?stopCode, scheduled], T0 )  
  event( stop_leave[?id, ?vehicle, ?stopCode, scheduled], T1 )  
  T1 > T0  
  end - start in [1, 2000]  
}
```

```
chronicle non_punctual[?id, ?vehicle]() {  
  event( stop_enter[?Id, ?vehicle, *, late], T0 )  
}
```

```
chronicle punctuality_change[?id, ?vehicle, non_punctual](T1) {  
  event( punctual[?id, ?vehicle], T0 )  
  event( non_punctual[?id, ?vehicle], T1 )  
  T1 > T0  
  noevent( punctual[?id, ?vehicle], ( T0+1, T1 ) )  
  noevent( non_punctual[?id, ?vehicle], ( T0+1, T1 ) )  
  end - start in [1, 20000]  
}
```

Chronicle Representation Language

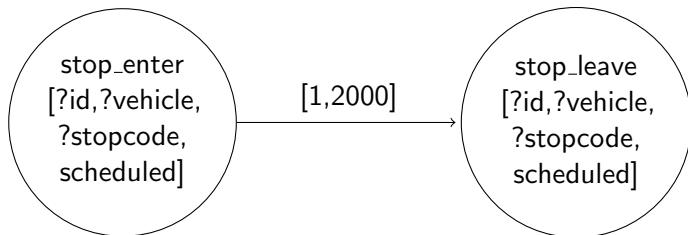
- ▶ Mathematical operators in the atemporal constraints of the language are not allowed:
 - ▶ cannot express that passenger safety is compromised more when a vehicle accident takes place **far** from a hospital or a police station.
- ▶ Universal quantification is not allowed:
 - ▶ cannot express that a route is punctual if **all** buses of the route are punctual.

CRS is a purely temporal reasoning system.

It is also a very efficient and scalable system.

Chronicle Recognition System: Semantics

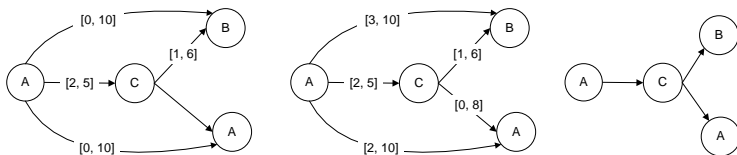
Each HLE definition is represented as a Temporal Constraint Network. Eg:



Chronicle Recognition System: Consistency Checking

Compilation stage:

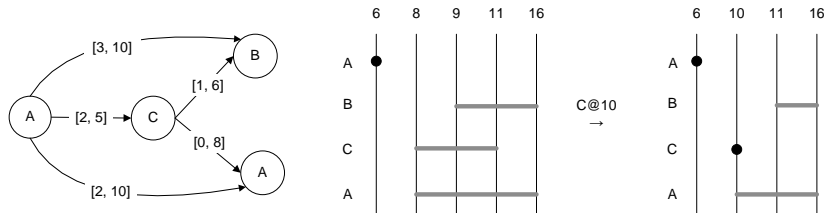
- Constraint propagation in the Temporal Constraint Network.
- Consistency checking.



Chronicle Recognition System: Recognition

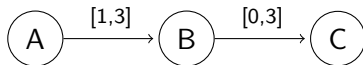
Recognition stage:

- ▶ Partial HLE instance evolution.
- ▶ Forward (predictive) recognition.



Chronicle Recognition System: Partial instances

HLE definition: Reduce tram endurance



A: enter tram intersection

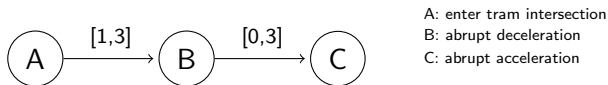
B: abrupt deceleration

C: abrupt acceleration



Chronicle Recognition System: Partial instances

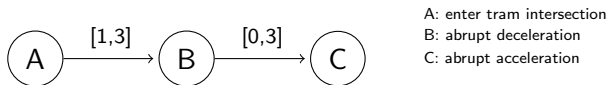
HLE definition: Reduce tram endurance



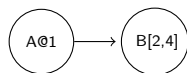
A@1 *time*

Chronicle Recognition System: Partial instances

HLE definition: Reduce tram endurance

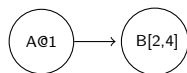
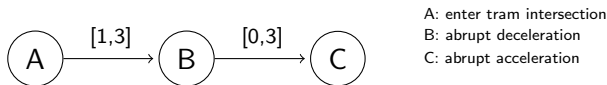


A@1 *time* →



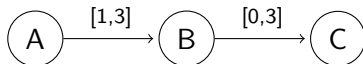
Chronicle Recognition System: Partial instances

HLE definition: Reduce tram endurance



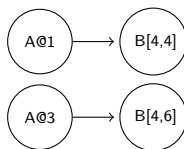
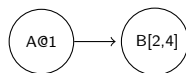
Chronicle Recognition System: Partial instances

HLE definition: Reduce tram endurance



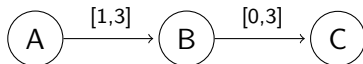
A: enter tram intersection
B: abrupt deceleration
C: abrupt acceleration

A@1 A@3 *time* →

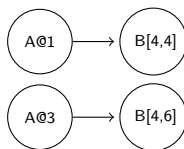
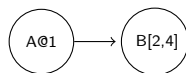


Chronicle Recognition System: Partial instances

HLE definition: Reduce tram endurance

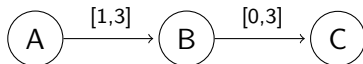


A: enter tram intersection
B: abrupt deceleration
C: abrupt acceleration

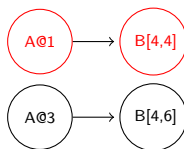
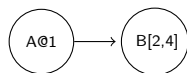


Chronicle Recognition System: Partial instances

HLE definition: Reduce tram endurance

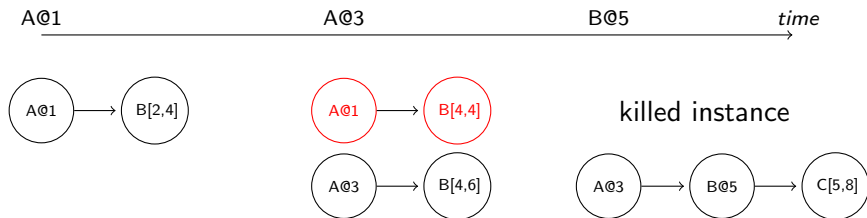
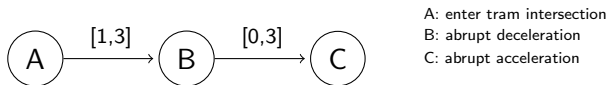


A: enter tram intersection
B: abrupt deceleration
C: abrupt acceleration



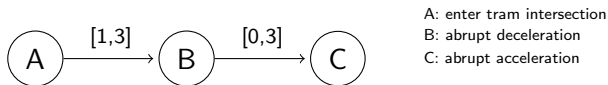
Chronicle Recognition System: Partial instances

HLE definition: Reduce tram endurance



Chronicle Recognition System: Partial instances

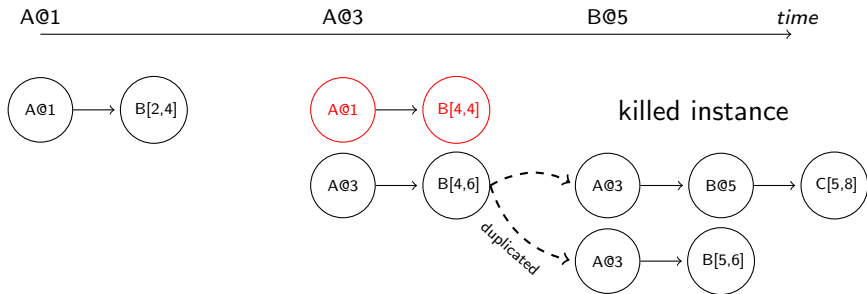
HLE definition: Reduce tram endurance



A: enter tram intersection

B: abrupt deceleration

C: abrupt acceleration



Chronicle Recognition System

Recognition stage — partial HLE instance management:

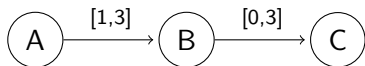
- ▶ In order to manage all the partial HLE instances, CRS stores them in trees, one for each HLE definition.
- ▶ Each event occurrence and each clock tick traverses these trees in order to kill some HLE instances (tree nodes) or to develop some HLE instances.
- ▶ For K HLE instances, each having n subevents, the complexity of processing each incoming event or a clock update is $O(Kn^2)$.
- ▶ To deal with out-of-order LLE streams, CRS keeps in memory partial HLE instances longer.

Chronicle Recognition System: Optimisation

Several techniques have been developed for improving efficiency.

Eg, 'temporal focusing':

- ▶ Distinguish between very rare events and frequent events based on a priori knowledge.
- ▶ Focus on the rare events: If, according to a HLE definition, a rare event should take place after the frequent event, store the incoming frequent events, and start recognition only upon the arrival of the rare event.
- ▶ This way the number of partial HLE instances is significantly reduced.
- ▶ Example: Reduce tram endurance



A: enter tram intersection

B: abrupt deceleration

C: abrupt acceleration

Chronicle Recognition System: Summary

- ▶ One of the earliest and most successful formal event processing systems.
- ▶ Being AI-based, it has been largely overlooked by the event processing community.
- ▶ Very efficient and scalable event recognition.
- ▶ But:
 - ▶ It is a purely temporal reasoning system.
 - ▶ It does not handle uncertainty.

Event Calculus

- ▶ A logic programming language for representing and reasoning about events and their effects.
- ▶ Key components:
 - ▶ event (typically instantaneous).
 - ▶ fluent: a property that may have different values at different points in time.
- ▶ Built-in representation of **inertia**:
 - ▶ $F = V$ holds at a particular time-point if $F = V$ has been *initiated* by an event at some earlier time-point, and not *terminated* by another event in the meantime.

HLE Definitions in the Event Calculus

HLE definition:

leaving_object(*P*, *Obj*) **initiated** iff
 appear(*Obj*) **happens**,
 inactive(*Obj*) **holds**,
 close(*P*, *Obj*) **holds**,
 person(*P*) **holds**

leaving_object(*P*, *Obj*) **terminated** iff
 disappear(*Obj*) **happens**

HLE recognition:

- ▶ *leaving_object*(*P*, *Obj*) **holdsFor** *I*

HLE Definitions in the Event Calculus

HLE definition:

$punctuality(ID) = non_punctual$ **initiated** iff
 $enter_stop(ID, Stop, late)$ **happens** or
 $leave_stop(ID, Stop, early)$ **happens**

$punctuality(ID) = non_punctual$ **terminatedAt** T iff
 $enter_stop(ID, Stop, scheduled)$ **happensAt** T' ,
 $leave_stop(ID, Stop, scheduled)$ **happensAt** T ,
 $T > T'$

HLE recognition:

- ▶ $punctuality(ID) = non_punctual$ **holdsFor** I

HLE Definitions in the Event Calculus

HLE definition:

driving_quality(ID) = low iff
punctuality(ID) = non_punctual or
driving_style(ID) = unsafe

Compiled HLE definition:

driving_quality(ID) = low **holdsFor** $I_1 \cup I_2$ iff
punctuality(ID) = non_punctual **holdsFor** I_1 ,
driving_style(ID) = unsafe **holdsFor** I_2

HLE Definitions in the Event Calculus

HLE definition:

driving_quality(ID) = medium iff
punctuality(ID) = punctual,
driving_style(ID) = uncomfortable

Compiled HLE definition:

driving_quality(ID) = medium **holdsFor** $I_1 \cap I_2$ iff
punctuality(ID) = punctual **holdsFor** I_1 ,
driving_style(ID) = uncomfortable **holdsFor** I_2

HLE Definitions in the Event Calculus

HLE definition:

$fighting(P_1, P_2)$ iff
 $(abrupt(P_1) \text{ or } abrupt(P_2))$,
 $close(P_1, P_2)$,
 not $(inactive(P_1) \text{ or } inactive(P_2))$

Compiled HLE definition:

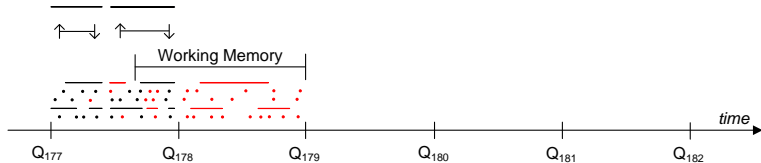
$fighting(P_1, P_2)$ **holdsFor** $((I_1 \cup I_2) \cap I_3) \setminus (I_4 \cup I_5)$ iff
 $abrupt(P_1)$ **holdsFor** I_1 ,
 $abrupt(P_2)$ **holdsFor** I_2 ,
 $close(P_1, P_2)$ **holdsFor** I_3 ,
 $inactive(P_1)$ **holdsFor** I_4 ,
 $inactive(P_2)$ **holdsFor** I_5

Run-Time Event Recognition

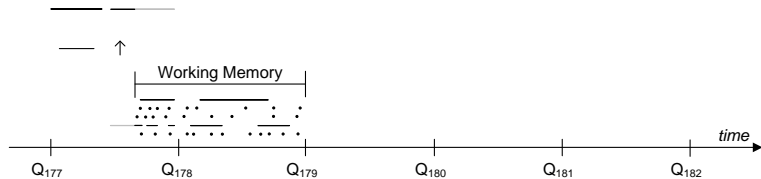
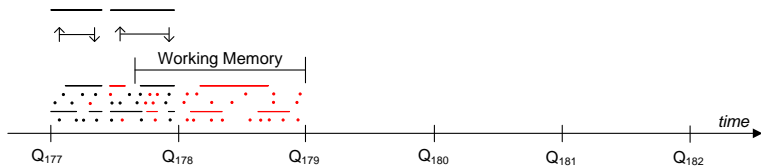
Real-time decision-support in the presence of:

- ▶ Very large LLE streams.
- ▶ Non-sorted LLE streams.
- ▶ LLE revision.
- ▶ Very large HLE numbers.

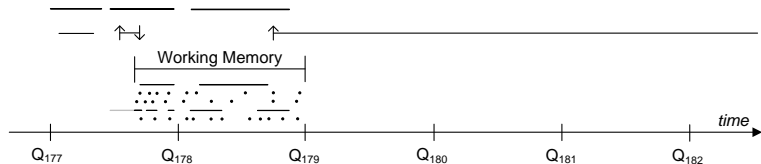
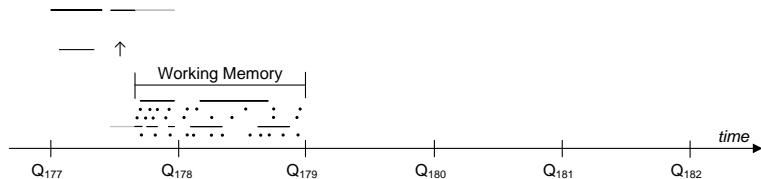
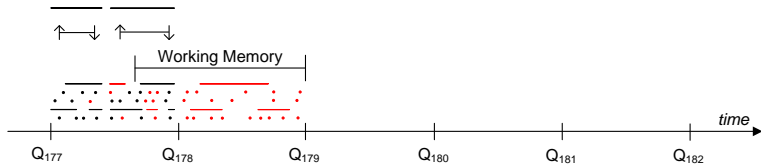
Event Calculus: Run-Time Event Recognition



Event Calculus: Run-Time Event Recognition



Event Calculus: Run-Time Event Recognition



Event Calculus: Summary

- ▶ Representation of complex temporal phenomena.
 - ▶ Succinct representation → code maintenance.
 - ▶ Intuitive representation → facilitates interaction with domain experts unfamiliar with programming.
- ▶ The full power of logic programming is available.
 - ▶ Complex atemporal computations in HLE definitions.
 - ▶ Combination of streaming data with historical knowledge.
- ▶ Very efficient reasoning.
 - ▶ Even when LLE arrive with a delay and are revised.
 - ▶ Even in the presence of large HLE hierarchies.
- ▶ But:
 - ▶ The Event Calculus has to deal with uncertainty.

Tutorial Structure

- ▶ Temporal reasoning systems.
- ▶ Event recognition under uncertainty.
- ▶ Machine learning for event recognition.
- ▶ Open issues.

Common Problems of Event Recognition

- ▶ Limited dictionary of LLE and context variables.
 - ▶ No explicit representation of hand shaking, falling down, etc.
- ▶ Incomplete LLE stream.
 - ▶ Abrupt acceleration was not detected.
- ▶ Erroneous LLE detection.
 - ▶ Abrupt acceleration was classified as sharp turn.
- ▶ Inconsistent ground truth (HLE & LLE annotation).
 - ▶ Disagreement between (human) annotators.

Therefore, an adequate treatment of uncertainty is required.

Logic-based models & Probabilistic models

- ▶ Logic-based models:
 - ▶ Very expressive with formal declarative semantics
 - ▶ Directly exploit background knowledge
 - ▶ Trouble with uncertainty
- ▶ Probabilistic graphical models:
 - ▶ Handle uncertainty
 - ▶ Lack of a formal representation language
 - ▶ Difficult to model complex events
 - ▶ Difficult to integrate background knowledge

Can these approaches combined?

Research communities that try combine these approaches:

- ▶ Probabilistic (Inductive) Logic Programming
- ▶ Statistical Relational Learning

How?

- ▶ Logic-based approaches incorporate statistical methods
- ▶ Probabilistic approaches learn logic-based models

ProbLog

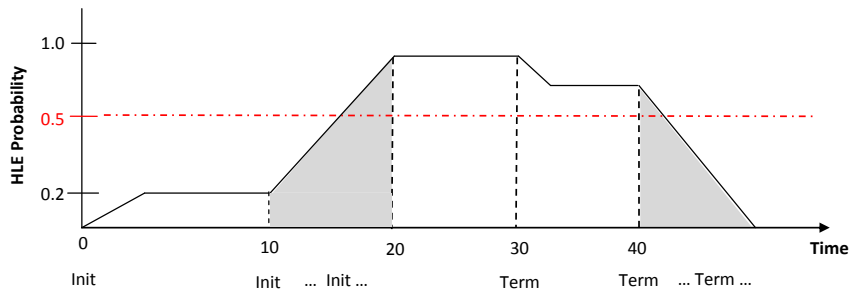
- ▶ A Probabilistic Logic Programming language.
- ▶ Allows for independent 'probabilistic facts' *prob::fact*.
- ▶ *Prob* indicates the probability that *fact* is part of a possible world.
- ▶ Rules are written as in classic Prolog.
- ▶ The probability of a query *q* imposed on a ProbLog database (*success probability*) is computed by the following formula:

$$P_s(q) = P\left(\bigvee_{e \in \text{Proofs}(q)} \bigwedge_{f_i \in e} f_i\right)$$

Event Recognition using ProbLog

Input	Output
340 0.45 :: <i>inactive</i> (id_0)	340 0.41 :: <i>leaving_object</i> (id_1, id_0)
340 0.80 :: $p(id_0) = (20.88, -11.90)$	340 0.55 :: <i>moving</i> (id_2, id_3)
340 0.55 :: <i>appear</i> (id_0)	
340 0.15 :: <i>walking</i> (id_2)	
340 0.80 :: $p(id_2) = (25.88, -19.80)$	
340 0.25 :: <i>active</i> (id_1)	
340 0.66 :: $p(id_1) = (20.88, -11.90)$	
340 0.70 :: <i>walking</i> (id_3)	
340 0.46 :: $p(id_3) = (24.78, -18.77)$	
...	

Event Calculus in ProbLog

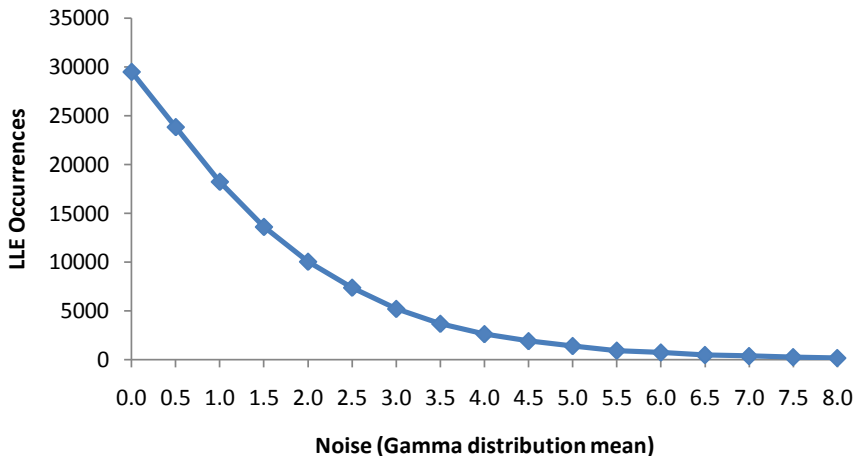


Event Calculus in ProbLog: Experimental Evaluation

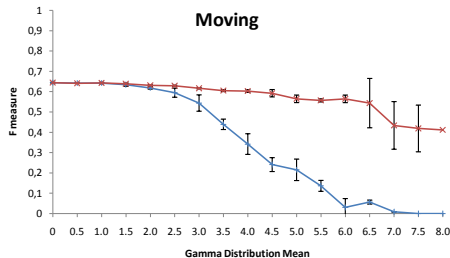
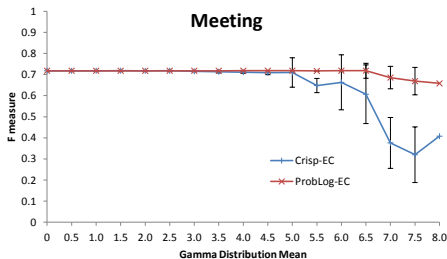
To compare ProbLog-EC to Crisp-EC:

- ▶ We add noise (probabilities) in LLE:
 - ▶ Crisp-EC: LLE with probability < 0.5 are discarded.
 - ▶ ProbLog-EC: all LLE are kept with their probabilities.
- ▶ In ProbLog-EC we accept as recognised the HLE that have probability > 0.5 .

Event Calculus in ProbLog: Experimental Evaluation

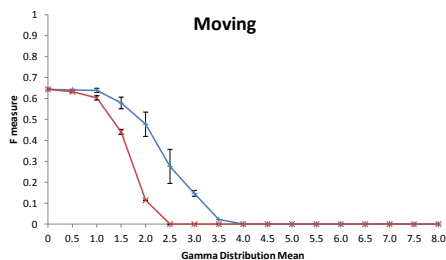
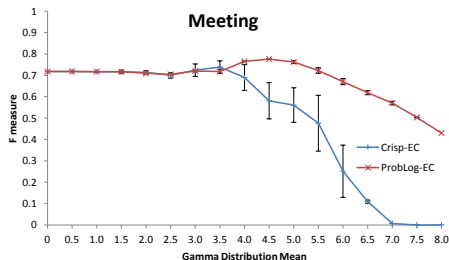


Event Calculus in ProbLog: Experimental Evaluation



moving(P_1, P_2) **initiated** iff
 walking(P_1) **happens**,
 walking(P_2) **happens**,
 close(P_1, P_2) **holds**,
 orientation(P_1) = O_1 **holds**,
 orientation(P_2) = O_2 **holds**,
 $|O_1 - O_2| < threshold$

Event Calculus in ProbLog: Experimental Evaluation

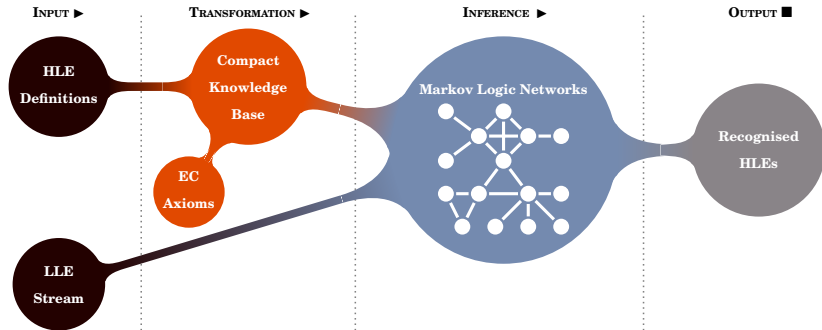


moving(P_1, P_2) **initiated** iff
walking(P_1) **happens**,
walking(P_2) **happens**,
close(P_1, P_2) **holds**,
orientation(P_1) = O_1 **holds**,
orientation(P_2) = O_2 **holds**,
 $|O_1 - O_2| < threshold$

Event Calculus in ProbLog: Summary

- ▶ ProbLog-EC clearly outperforms Crisp-EC when:
 - ▶ The environment is highly noisy ($LLE < 0.5$) — realistic assumption in many domains,
 - ▶ there are successive initiations that allow the HLE's probability to increase and eventually exceed the specified (0.5) threshold, and
 - ▶ the amount of probabilistic conjuncts in an initiation condition is limited.
- ▶ Note that:
 - ▶ we also need to deal with uncertainty in the HLE definitions.

Markov Logic Networks (MLN)



- ▶ Syntax: weighted first-order logic formulas (F_i, w_i) .
- ▶ Semantics: (F_i, w_i) represents a probability distribution over possible worlds.
- ▶ A world violating formulas becomes less probable, but not impossible.

Markov Logic: Representation

Example definition of HLE 'uncomfortable_driving' :

w_1 $abrupt_movement(Id, Vehicle, T) \leftarrow$
 $abrupt_acceleration(Id, Vehicle, T) \vee$
 $abrupt_deceleration(Id, Vehicle, T) \vee$
 $sharp_turn(Id, Vehicle, T)$

w_2 $uncomfortable_driving(Id, Vehicle, T_2) \leftarrow$
 $approach_intersection(Id, Vehicle, T_1) \wedge$
 $abrupt_movement(Id, Vehicle, T_2) \wedge$
 $before(T_1, T_2)$

Markov Logic: Representation

- ▶ Weight: a real-valued number.
- ▶ Higher weight \longrightarrow Stronger constraint
- ▶ Hard constraints
 - ▶ Infinite weight values.
 - ▶ Background knowledge.
- ▶ Soft constraints
 - ▶ Strong weight values: almost always true.
 - ▶ Weak weight values: describe exceptions.

Markov Logic: Network Construction

- ▶ Formulas are translated into clausal form.
- ▶ Weights are divided equally among clauses:

$$\frac{1}{3} w_1 \quad \neg abrupt_acceleration(Id, Vehicle, T) \vee abrupt_movement(Id, Vehicle, T)$$

$$\frac{1}{3} w_1 \quad \neg abrupt_deceleration(Id, Vehicle, T) \vee abrupt_movement(Id, Vehicle, T)$$

$$\frac{1}{3} w_1 \quad \neg sharp_turn(Id, Vehicle, T) \vee abrupt_movement(Id, Vehicle, T)$$

$$w_2 \quad \neg approach_intersection(Id, Vehicle, T_1) \vee \neg abrupt_movement(Id, Vehicle, T_2) \vee \neg before(T_1, T_2) \vee uncomfortable_driving(Id, Vehicle, T_2)$$

Markov Logic: Network Construction

Template that produces ground Markov network:

- ▶ Given a set of constants from the input LLE stream
 - ▶ Ground all clauses.
- ▶ Boolean nodes: ground predicates.
- ▶ Each ground clause:
 - ▶ Forms a clique in the network.
 - ▶ Is associated with w_i and a Boolean feature.

$$P(X = x) = \frac{1}{Z} \exp \left(\sum_i w_i n_i(x) \right)$$

$$Z = \sum_{x \in \mathcal{X}} \exp(P(X = x))$$

Markov Logic: Network Construction

$$\frac{1}{3}w_1 \quad \neg abrupt_acceleration(Id, Vehicle, T) \vee abrupt_movement(Id, Vehicle, T)$$

$$\frac{1}{3}w_1 \quad \neg abrupt_deceleration(Id, Vehicle, T) \vee abrupt_movement(Id, Vehicle, T)$$

$$\frac{1}{3}w_1 \quad \neg sharp_turn(Id, Vehicle, T) \vee abrupt_movement(Id, Vehicle, T)$$

$$w_2 \quad \neg approach_intersection(Id, Vehicle, T_1) \vee \neg abrupt_movement(Id, Vehicle, T_2) \vee \\ \neg before(T_1, T_2) \vee uncomfortable_driving(Id, Vehicle, T_2)$$

LLE:

abrupt_acceleration(*tr*₀, *tram*, 101)
approach_intersection(*tr*₀, *tram*, 100)
before(100, 101)

Constants:

T = {100, 101}
Id = {*tr*₀}
Vehicle = {*tram*}

Markov Logic: Network Construction

For example, the clause:

$$w_2 \quad \neg \text{approach_intersection}(Id, Vehicle, T_1) \vee \neg \text{abrupt_movement}(Id, Vehicle, T_2) \vee \neg \text{before}(T_1, T_2) \vee \text{uncomfortable_driving}(Id, Vehicle, T_2)$$

produces the following groundings:

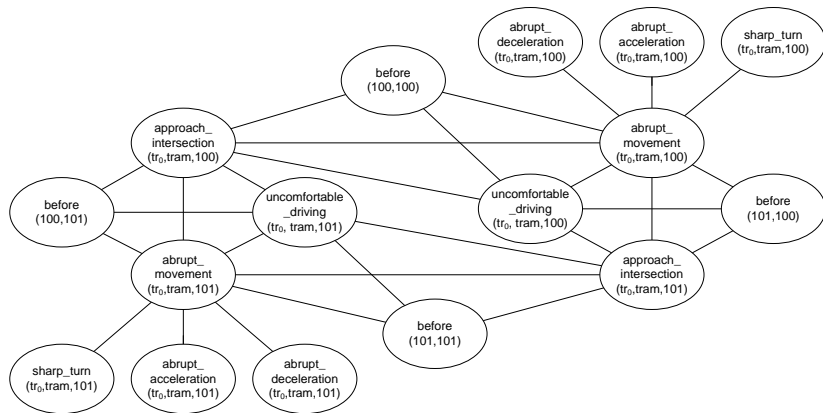
$$w_2 \quad \neg \text{approach_intersection}(tr_0, tram, 100) \vee \neg \text{abrupt_movement}(tr_0, tram, 100) \vee \neg \text{before}(100, 100) \vee \text{uncomfortable_driving}(tr_0, tram, 100)$$

$$w_2 \quad \neg \text{approach_intersection}(tr_0, tram, 100) \vee \neg \text{abrupt_movement}(tr_0, tram, 101) \vee \neg \text{before}(100, 101) \vee \text{uncomfortable_driving}(tr_0, tram, 101)$$

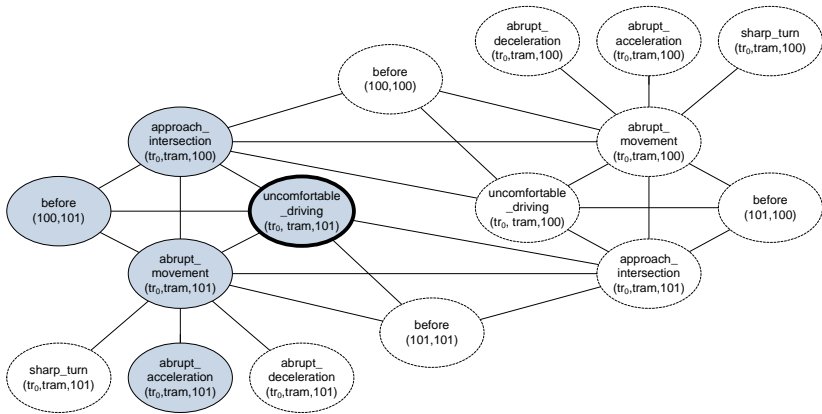
$$w_2 \quad \neg \text{approach_intersection}(tr_0, tram, 101) \vee \neg \text{abrupt_movement}(tr_0, tram, 100) \vee \neg \text{before}(101, 100) \vee \text{uncomfortable_driving}(tr_0, tram, 100)$$

$$w_2 \quad \neg \text{approach_intersection}(tr_0, tram, 101) \vee \neg \text{abrupt_movement}(tr_0, tram, 101) \vee \neg \text{before}(101, 101) \vee \text{uncomfortable_driving}(tr_0, tram, 101)$$

Markov Logic: Network Construction

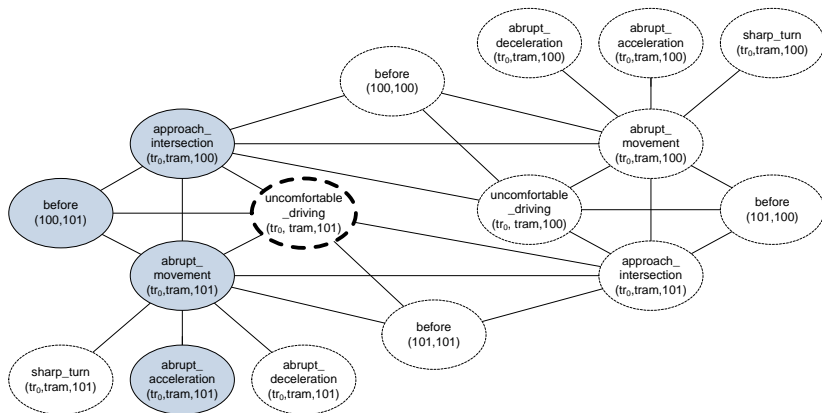


Markov Logic: World state discrimination



$$P(X=x_1) = \frac{1}{7} \exp(\frac{1}{3} w_1 \cdot 2 + \frac{1}{3} w_1 \cdot 2 + \frac{1}{3} w_1 \cdot 2 + w_2 \cdot 4) = \frac{1}{7} e^{2w_1 + 4w_2}$$

Markov Logic: World state discrimination



$$P(X = x_1) = \frac{1}{Z} \exp\left(\frac{1}{3} w_1 \cdot 2 + \frac{1}{3} w_1 \cdot 2 + \frac{1}{3} w_1 \cdot 2 + w_2 \cdot 4\right) = \frac{1}{Z} e^{2w_1 + 4w_2}$$

$$P(X = x_2) = \frac{1}{Z} \exp\left(\frac{1}{3} w_1 \cdot 2 + \frac{1}{3} w_1 \cdot 2 + \frac{1}{3} w_1 \cdot 2 + w_2 \cdot 3\right) = \frac{1}{Z} e^{2w_1 + 3w_2}$$

Markov Logic: Inference

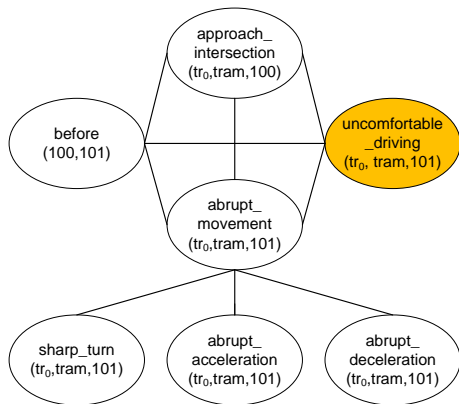
- ▶ Event recognition involves querying about HLE.
- ▶ Given a ground Markov network, apply standard probabilistic inference methods.
- ▶ Markov network may be large and have a complex structure
 - ▶ Inference may become infeasible.
- ▶ MLN combine logical and probabilistic inference methods.

Markov Logic: Conditional inference

Query: Which trams are driven in an uncomfortable manner?

- Query variables Q : HLE

$$P(Q \mid E = e) = \frac{P(Q, E = e, H)}{P(E = e, H)}$$

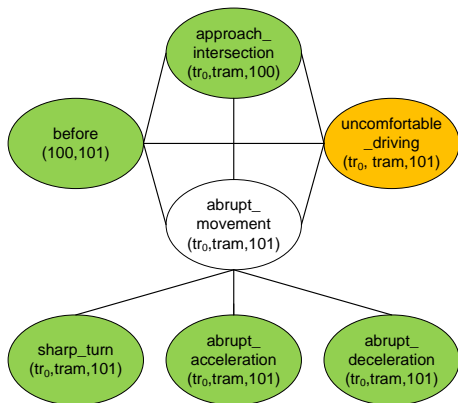


Markov Logic: Conditional inference

Query: Which trams are driven in an uncomfortable manner?

- ▶ Query variables Q : HLE
- ▶ Evidence variables E : LLE

$$P(Q \mid E = e) = \frac{P(Q, E = e, H)}{P(E = e, H)}$$

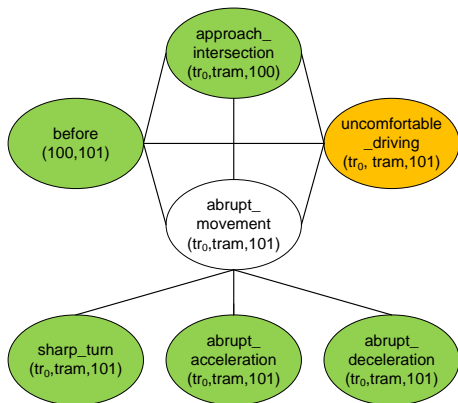


Markov Logic: Conditional inference

Query: Which trams are driven in an uncomfortable manner?

- ▶ Query variables Q : HLE
- ▶ Evidence variables E : LLE
- ▶ Hidden variables H

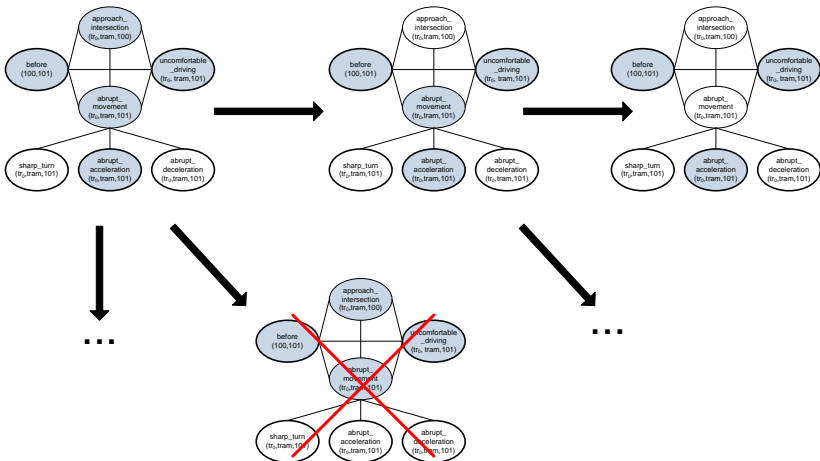
$$P(Q \mid E = e) = \frac{P(Q, E = e, H)}{P(E = e, H)}$$



Markov Logic: Conditional inference

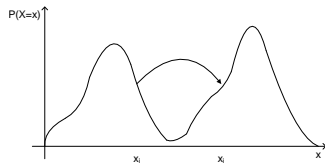
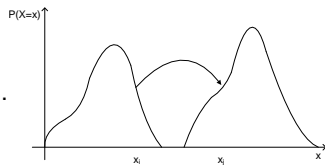
- ▶ Efficiently approximated with sampling.
- ▶ Markov Chain Monte Carlo (MCMC): e.g Gibbs sampling.
- ▶ Random walks in state space.
- ▶ Reject all states where $E = e$ does not hold.

Markov Logic: MCMC

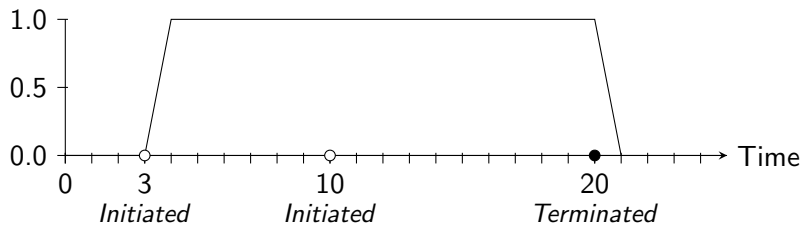


Markov Logic: Deterministic dependencies

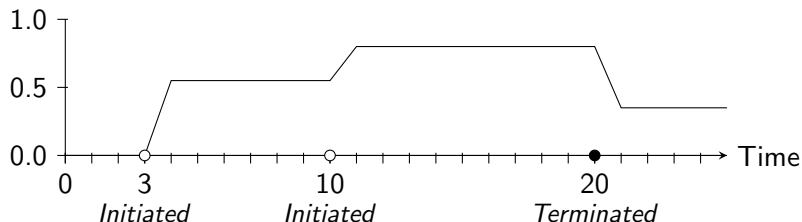
- ▶ MCMC is a pure statistical method.
- ▶ MLN combine logic and probabilistic models.
- ▶ Hard constrained formulas:
 - ▶ Deterministic dependencies.
 - ▶ Isolated regions in state space.
- ▶ Strong constrained formulas:
 - ▶ Near-deterministic dependencies.
 - ▶ Difficult to cross regions.
- ▶ Combination of satisfiability testing with MCMC.



Event Calculus



Event Calculus in MLN



Hard-constrained inertia rules:

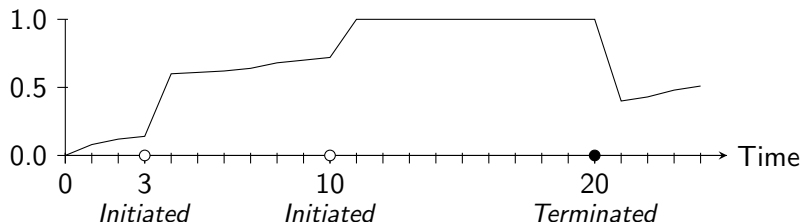
2.3 HLE **initiatedAt** T if
[Conditions]

$\neg(HLE \text{ holdsAt } T)$ iff
 $\neg(HLE \text{ holdsAt } T-1),$
 $\neg(HLE \text{ initiatedAt } T-1)$

2.5 HLE **terminatedAt** T if
[Conditions]

$HLE \text{ holdsAt } T$ iff
 $HLE \text{ holdsAt } T-1,$
 $\neg(HLE \text{ terminatedAt } T-1)$

Event Calculus in MLN



Soft-constrained initiation inertia rules:

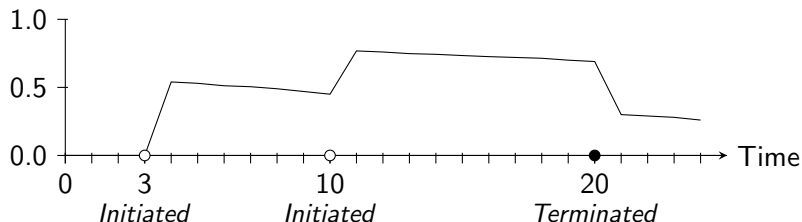
2.3 $HLE \text{ initiatedAt } T$ if
[Conditions]

2.5 $HLE \text{ terminatedAt } T$ if
[Conditions]

2.8 $\neg(HLE \text{ holdsAt } T)$ iff
 $\neg(HLE \text{ holdsAt } T-1),$
 $\neg(HLE \text{ initiatedAt } T-1)$

$HLE \text{ holdsAt } T$ iff
 $HLE \text{ holdsAt } T-1,$
 $\neg(HLE \text{ terminatedAt } T-1)$

Event Calculus in MLN



Soft-constrained termination inertia rules:

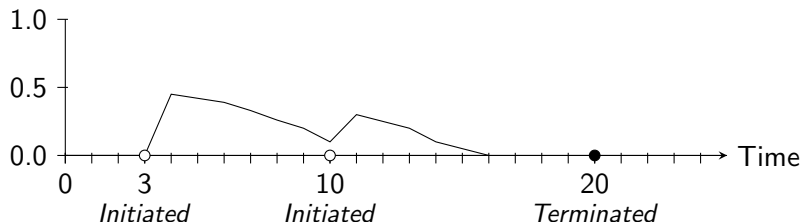
2.3 HLE **initiatedAt** T if
[Conditions]

2.5 HLE **terminatedAt** T if
[Conditions]

$\neg(HLE$ **holdsAt** $T)$ iff
 $\neg(HLE$ **holdsAt** $T-1)$,
 $\neg(HLE$ **initiatedAt** $T-1)$

2.8 HLE **holdsAt** T iff
 HLE **holdsAt** $T-1$,
 $\neg(HLE$ **terminatedAt** $T-1)$

Event Calculus in MLN



Soft-constrained termination inertia rules:

2.3 HLE **initiatedAt** T if
[Conditions]

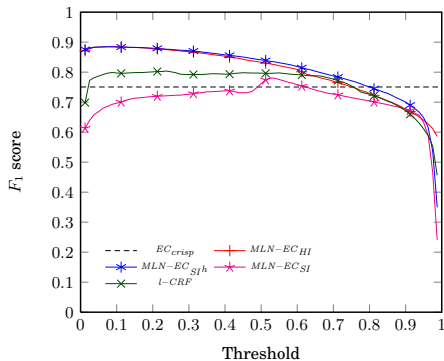
2.5 HLE **terminatedAt** T if
[Conditions]

$\neg(HLE$ **holdsAt** $T)$ iff
 $\neg(HLE$ **holdsAt** $T-1)$,
 $\neg(HLE$ **initiatedAt** $T-1)$

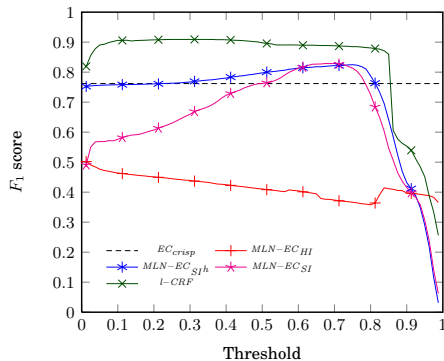
0.8 HLE **holdsAt** T iff
 HLE **holdsAt** $T-1$,
 $\neg(HLE$ **terminatedAt** $T-1)$

Event Calculus in MLN: Experimental Evaluation

Moving



Meeting



Event Calculus in MLN: Summary

- ▶ We can deal with both:
 - ▶ Uncertainty in the HLE definitions, and
 - ▶ uncertainty in the input.
- ▶ Customisable inertia behaviour to meet the requirements of different applications.
- ▶ But:
 - ▶ There is room for improvement with respect to efficiency.

Event Recognition under Uncertainty

- ▶ Probabilistic reasoning improves recognition accuracy.
- ▶ But probabilistic reasoning often does not allow for real-time event recognition.
- ▶ Solution: **self-adaptive event recognition**
 - ▶ Streams from multiple sources are matched against each other to identify mismatches that indicate uncertainty in the sources.
 - ▶ Temporal regions of uncertainty are identified from which the system autonomously decides to adapt its event sources in order to deal with uncertainty, without compromising efficiency.
 - ▶ Data **variety** is used to handle **veracity**.

Self-Adaptive Event Recognition

busReportedCongestion(Lon, Lat) **initiated** iff
 move(Bus, Lon_B, Lat_B, 1) **happens**,
 close(Lon_B, Lat_B, Lon, Lat)

busReportedCongestion(Lon, Lat) **terminated** iff
 move(Bus, Lon_B, Lat_B, 0) **happens**,
 close(Lon_B, Lat_B, Lon, Lat)

Self-Adaptive Event Recognition: Identifying Mismatches among Different Streams

noisy(*Bus*) **initiated** iff
 move(*Bus*, *Lon_B*, *Lat_B*, 1) **happens**,
 close(*Lon_B*, *Lat_B*, *Lon_S*, *Lat_S*),
 \neg (*scatsReportedCongestion*(*Lon_S*, *Lat_S*) **holds**)

noisy(*Bus*) **terminated** if
 move(*Bus*, *Lon_B*, *Lat_B*, 1) **happens**,
 close(*Lon_B*, *Lat_B*, *Lon_S*, *Lat_S*),
 scatsReportedCongestion(*Lon_S*, *Lat_S*) **holds**

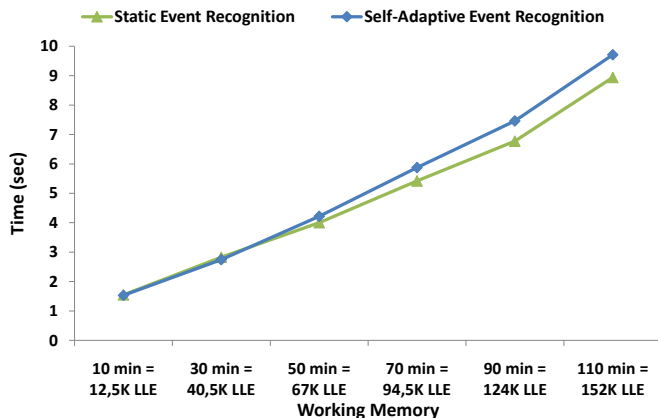
noisy(*Bus*) **terminated** if
 move(*Bus*, *Lon_B*, *Lat_B*, 0) **happens**,
 close(*Lon_B*, *Lat_B*, *Lon_S*, *Lat_S*),
 \neg (*scatsReportedCongestion*(*Lon_S*, *Lat_S*) **holds**)

Self-Adaptive Event Recognition: Discard Temporarily Unreliable Event Sources

busReportedCongestion(*Lon*, *Lat*) **initiated** iff
 move(*Bus*, *Lon_B*, *Lat_B*, 1) **happens**,
 \neg (*noisy*(*Bus*) **holds**),
 close(*Lon_B*, *Lat_B*, *Lon*, *Lat*)

busReportedCongestion(*Lon*, *Lat*) **terminated** iff
 move(*Bus*, *Lon_B*, *Lat_B*, 0) **happens**,
 \neg (*noisy*(*Bus*) **holds**),
 close(*Lon_B*, *Lat_B*, *Lon*, *Lat*)

Self-Adaptive Event Recognition in Dublin



Event Recognition Under Uncertainty: Summary

- ▶ Uncertainty in the input:
 - ▶ Probabilistic reasoning.
 - ▶ Using variety for veracity (when possible).
- ▶ Uncertainty in the HLE definitions:
 - ▶ Probabilistic reasoning.
- ▶ But:
 - ▶ We are still missing a framework for real-time, probabilistic event recognition.

Tutorial Structure

- ▶ Temporal reasoning systems.
- ▶ Event recognition under uncertainty.
- ▶ Machine learning for event recognition.
- ▶ Open issues.

Machine Learning for Event Recognition

Manual development of HLE definitions:

- ▶ Time consuming.
- ▶ Error-prone.

Automated construction for HLE definitions:

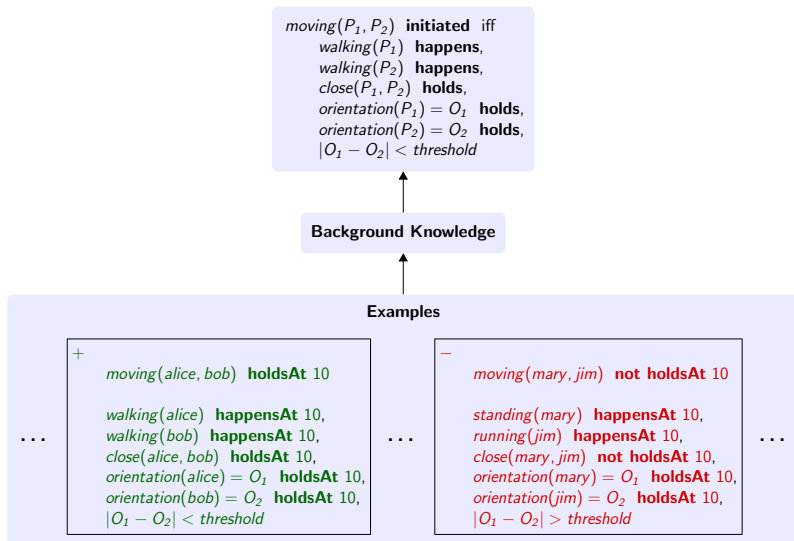
- ▶ Learn complex HLE definitions
 - ▶ Structure learning
- ▶ Learn from noisy data
 - ▶ Parameter learning
- ▶ Learn with incomplete or missing annotation
 - ▶ Semi-supervised, unsupervised learning
- ▶ Learn from large amounts of data
 - ▶ Scalable algorithms, incremental learning

Learning the Structure of HLE Definitions

Inductive Logic Programming (ILP):

- ▶ Input:
 - ▶ LLE streams annotated with HLE
 - ▶ Examples E^+ , E^- .
 - ▶ Event recognition engine
 - ▶ Background knowledge B .
 - ▶ Syntax of event recognition language
 - ▶ Language bias M .
- ▶ Output:
 - ▶ A HLE definition
 - ▶ Hypothesis H in the language of M such that $B \cup H$ entails all positive and none of the negative examples.

Learning the Structure of HLE Definitions with ILP



Learning HLE definitions with ILP

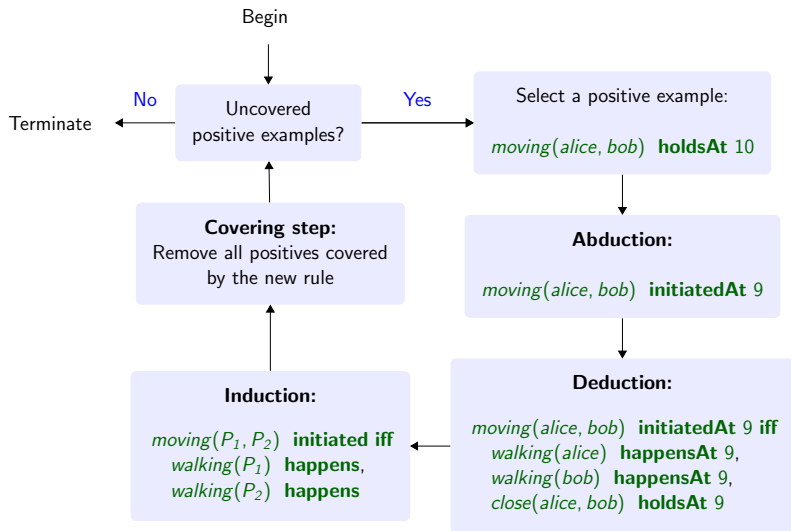
Non-Observational Predicate Learning:

- ▶ Supervision
 - ▶ **holdsAt**
- ▶ Target
 - ▶ **initiated, terminated**
- ▶ Traditional ILP systems cannot handle this

Solution:

- ▶ Obtain missing supervision by computing possible explanations of the examples ([Abduction](#)).

eXtended Hybrid Abductive-Inductive Learning – XHAIL

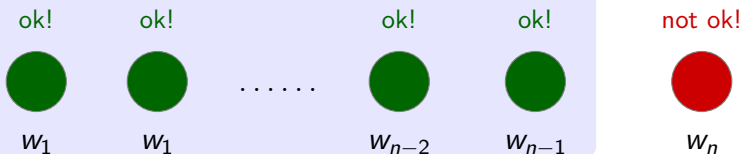


Incremental Learning

Given:

- ▶ A LLE stream \mathcal{E} annotated with HLE (historical memory)
- ▶ A HLE definition H which is **correct** w.r.t \mathcal{E}
- ▶ A new LLE batch in which H is **incorrect**

Historical Memory \mathcal{E}



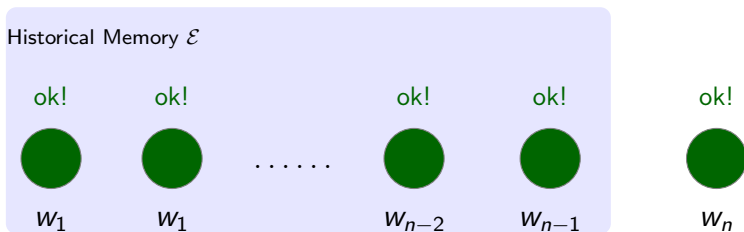
$H :$

fighting(P_1, P_2) **initiated iff**
active(P_1) **happens,**
abrupt(P_2) **happens**

Incremental Learning

Goal:

- Revise H to an H' that is correct w.r.t **all examples**

 $H' :$

fighting(P_1, P_2) **initiated iff**
active(P_1) **happens,**
abrupt(P_2) **happens,**
close(P_1, P_2) **holds**

<i>fighting</i> (P_1, P_2) initiated iff	<i>fighting</i> (P_1, P_2) initiated iff
<i>active</i> (P_1) happens,	<i>abrupt</i> (P_1) happens,
<i>abrupt</i> (P_2) happens,	<i>abrupt</i> (P_2) happens,
<i>close</i> (P_1, P_2) holds	<i>close</i> (P_1, P_2) holds

Incremental Learning

Specialisation:

- Reject negative examples

$H :$

fighting(P_1, P_2) **initiated iff**
active(P_1) **happens,**
abrupt(P_2) **happens**



$H' :$

fighting(P_1, P_2) **initiated iff**
active(P_1) **happens,**
abrupt(P_2) **happens,**
close(P_1, P_2) **holds**

Incremental Learning

Generalisation:

- Cover more positive examples

$H :$

fighting(P_1, P_2) **initiated iff**
active(P_1) **happens,**
abrupt(P_2) **happens,**
close(P_1, P_2) **holds**



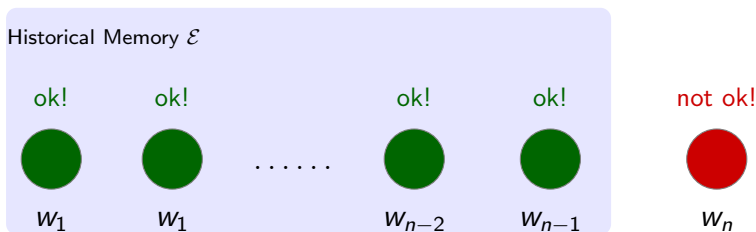
$H' :$

<i>fighting</i> (P_1, P_2) initiated iff <i>active</i> (P_1) happens, <i>abrupt</i> (P_2) happens, <i>close</i> (P_1, P_2) holds	<i>fighting</i> (P_1, P_2) initiated iff <i>abrupt</i> (P_1) happens, <i>abrupt</i> (P_2) happens, <i>close</i> (P_1, P_2) holds
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Incremental Learning is Hard

Example:

- Specialise a HLE definition



Negative examples covered

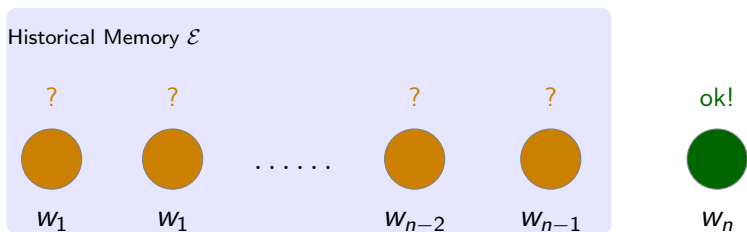
$H :$

fighting(P_1, P_2) **initiated iff**
active(P_1) **happens,**
abrupt(P_2) **happens**

Incremental Learning is Hard

Example:

- Specialise a HLE definition



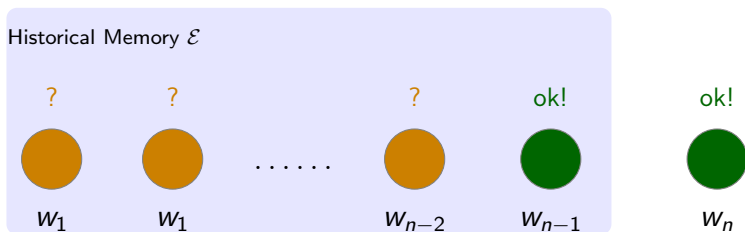
H' :

fighting(P_1, P_2) **initiated iff**
active(P_1) **happens,**
abrupt(P_2) **happens,**
close(P_1, P_2) **holds**

Incremental Learning is Hard

Example:

- Specialise a HLE definition



H' :

fighting(P_1, P_2) **initiated iff**
active(P_1) **happens,**
abrupt(P_2) **happens,**
close(P_1, P_2) **holds**

Incremental Learning is Hard

Example:

- Specialise a HLE definition

Historical Memory \mathcal{E}



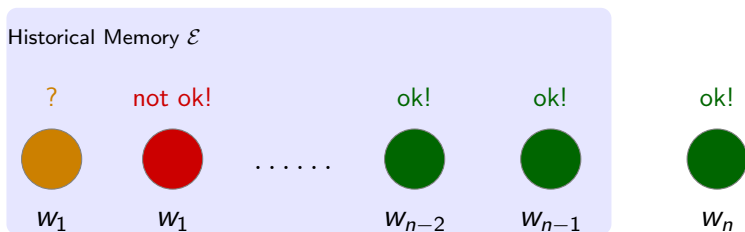
H' :

fighting(P_1, P_2) **initiated iff**
active(P_1) **happens,**
abrupt(P_2) **happens,**
close(P_1, P_2) **holds**

Incremental Learning is Hard

Example:

- Specialise a HLE definition



Positive examples not covered

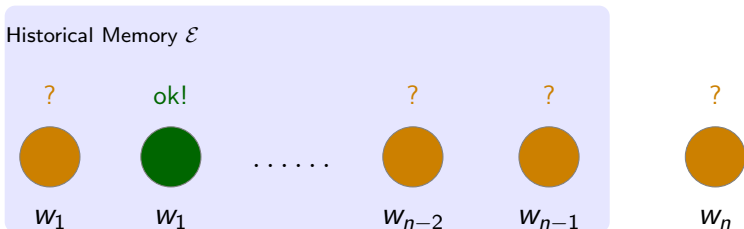
H' :

fighting(P_1, P_2) **initiated iff**
active(P_1) **happens,**
abrupt(P_2) **happens,**
close(P_1, P_2) **holds**

Incremental Learning is Hard

Example:

- Specialise a HLE definition



We must start all over again...

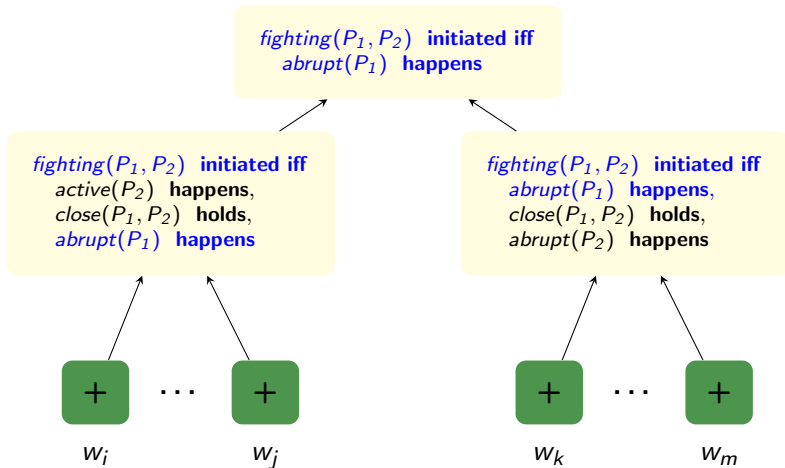
H'' :

fighting(P_1, P_2) **initiated iff** *active*(P_1) **happens,**
abrupt(P_2) **happens,**
close(P_1, P_2) **holds**

fighting(P_1, P_2) **initiated iff**
abrupt(P_1) **happens**

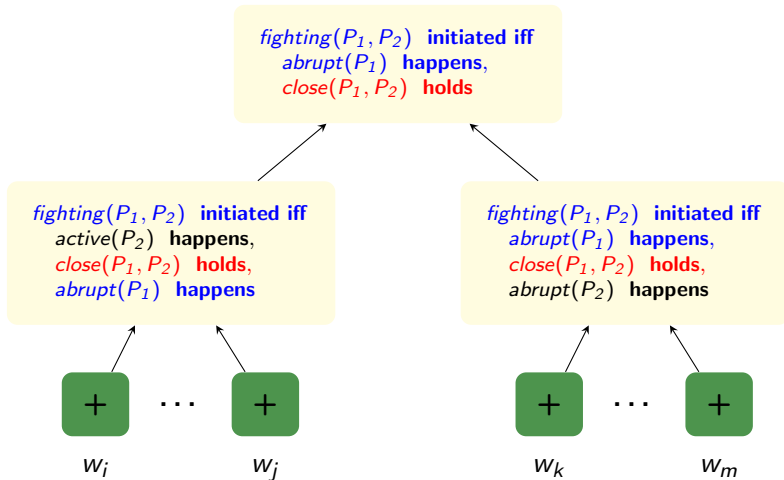
Efficient Incremental Learning: Support Set

- ▶ While constructing a HLE definition, summarize the positive examples it covers so far.
- ▶ This memory can be used for specialisation without having to look back.



Support Set

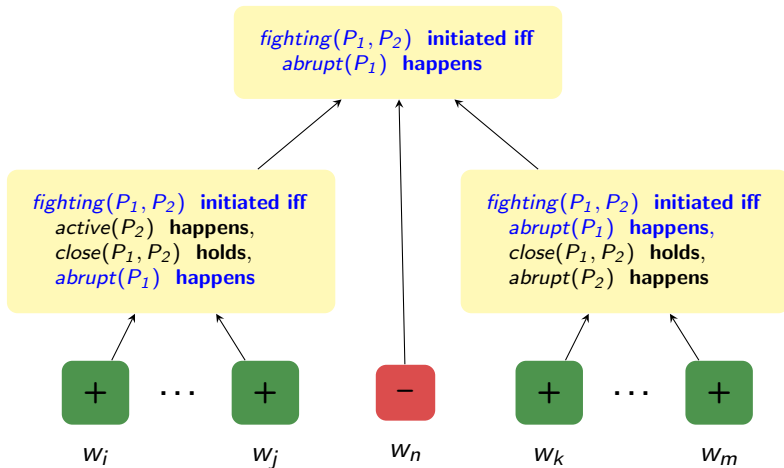
- ▶ To revise a HLE definition while preserving the positive examples it covers
 - ▶ It suffices for the revision to **subsume the support set**



Support Set Example

Find the smallest set of “supported” specialisations such that:

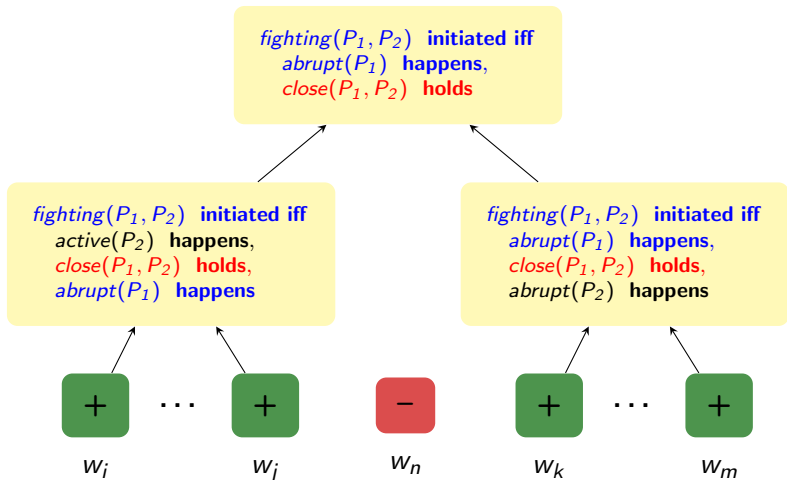
- ▶ All specialisations subsume the support set.
- ▶ Each specialisation rejects the negative examples.



Support Set Example

Find the smallest set of “supported” specialisations such that:

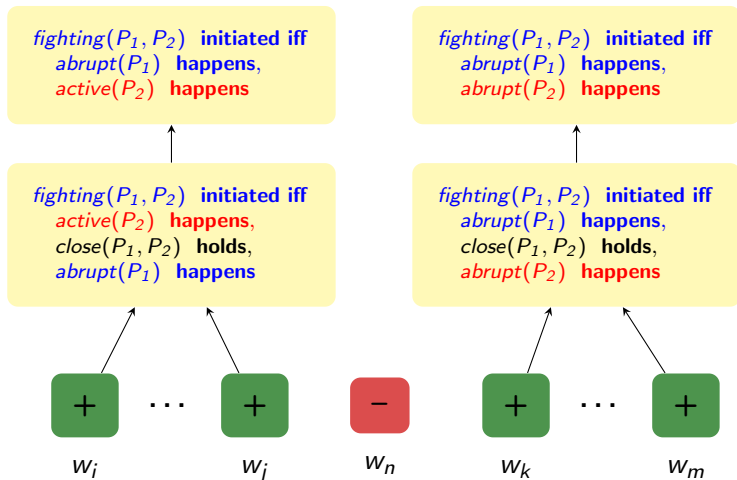
- ▶ All specialisations subsume the support set.
- ▶ Each specialisation rejects the negative examples.
- ▶ A single specialisation may suffice.



Support Set Example

Find the smallest set of “supported” specialisations such that:

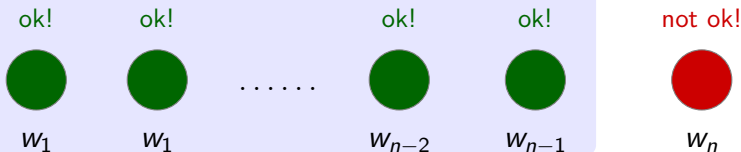
- ▶ All specialisations subsume the support set.
- ▶ Each specialisation rejects the negative examples.
- ▶ The HLE definition may need to “split”.



What do we achieve?

- Without the support set

Historical Memory \mathcal{E}



Negative examples covered

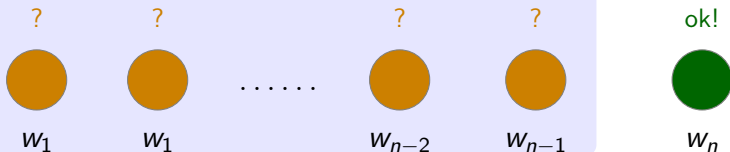
$H :$

fighting(P_1, P_2) **initiated iff**
abrupt(P_1) **happens**

What do we achieve?

- Without the support set

Historical Memory \mathcal{E}



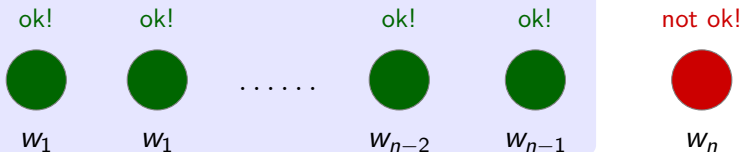
H' :

fighting(P_1, P_2) **initiated iff**
abrupt(P_1) **happens,**
active(P_2) **happens**

What do we achieve?

- With the support set

Historical Memory \mathcal{E}



Negative examples covered

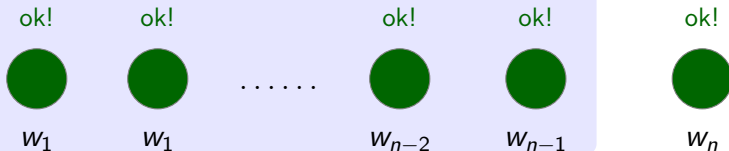
$H :$

fighting(P_1, P_2) **initiated iff**
abrupt(P_1) **happens**

What do we achieve?

- ▶ **With** the support set
 - ▶ Reject negative examples locally, preserve positive examples globally.
 - ▶ Reasoning within the support set, avoid redundant inference in the historical memory
 - ▶ At most one pass over the historical memory is required.

Historical Memory \mathcal{E}



H' :

fighting(P_1, P_2) **initiated** iff *fighting*(P_1, P_2) **initiated** iff
abrupt(P_1) **happens**, *abrupt*(P_1) **happens**,
active(P_2) **happens** *abrupt*(P_2) **happens**

Machine Learning for Event Recognition: Summary

- ▶ Automated construction & refinement of HLE definitions
 - ▶ Taking advantage of very large datasets.
 - ▶ Dealing with partial supervision.
- ▶ But:
 - ▶ We also need to deal with noise
 - ▶ Simultaneous optimisation of structure and parameters.

Tutorial Structure

- ▶ Temporal reasoning systems.
- ▶ Event recognition under uncertainty.
- ▶ Machine learning for event recognition.
- ▶ Open issues.

Open Issues

- ▶ Machine learning under uncertainty.
- ▶ Real-time event recognition under uncertainty.
- ▶ Distributed event recognition.
- ▶ Multi-scale temporal aggregation of events.
- ▶ Event forecasting under uncertainty.
- ▶ User-friendly authoring tools enabling non-programmers to use event recognition & forecasting.

Tutorial Resources

- ▶ Alexander Artikis, Anastasios Skarlatidis, Francois Portet, Georgios Paliouras: Logic-based event recognition. Knowledge Engineering Review 27(4): 469-506 (2012).
- ▶ Software, datasets, slides & papers at cer.iit.demokritos.gr