

# Online Reasoning under Uncertainty with the Event Calculus

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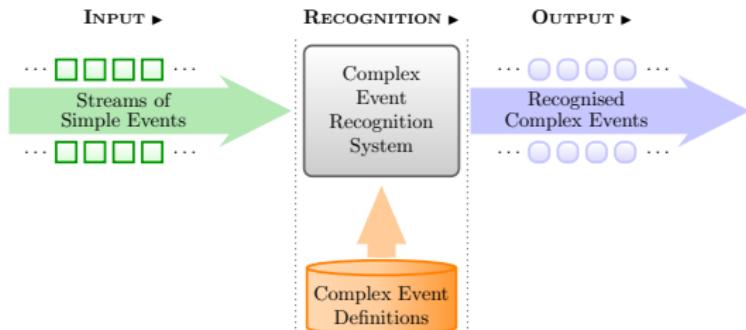
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<http://cer.iit.demokritos.gr/>

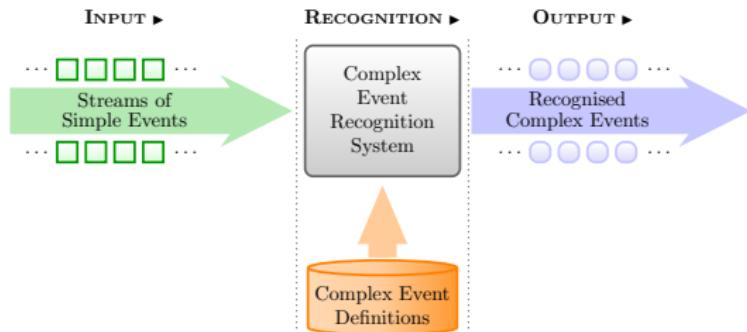


# Complex Event Recognition (Event Pattern Matching)



Giatrakos et al, *Complex event recognition in the Big Data era: a survey*, VLDB Journal, 2020.

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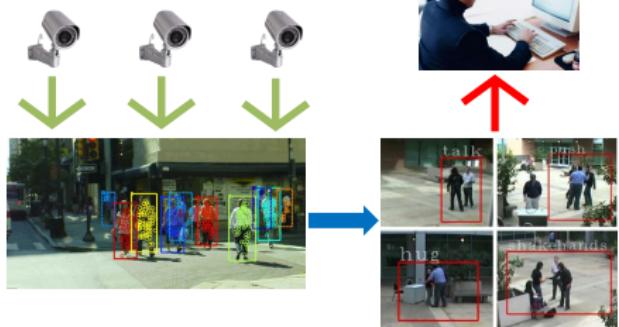
Giatrakos et al, Complex event recognition in the Big Data era: a survey, VLDB Journal, 2020.

<https://rdcu.be/cNkQE>

# Human Activity Recognition



# Human Activity Recognition



<https://cer.iit.demokritos.gr> (activity recognition)

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  - to capture complex relationships between the events that stream into the system.

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# Event Calculus

- A logic programming language for representing and reasoning about events and their effects.
- Key components:
  - event (typically instantaneous).
  - fluent: a property that may have different values at different points in time.

*Kowalski and Sergot, A Logic-based Calculus of Events. New Generation Computing, 1986.*

# Event Calculus

- A logic programming language for representing and reasoning about events and their effects.
- Key components:
  - event (typically instantaneous).
  - fluent: a property that may have different values at different points in time.
- Built-in representation of inertia:
  - $F = V$  holds at a particular time-point if  $F = V$  has been *initiated* by an event at some earlier time-point, and not *terminated* by another event in the meantime.

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# Online Probabilistic Event Calculus

Prob-EC =  
Event Calculus  
+ ProbLog

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## Event Calculus Axioms

```
holdsAt( $F = V, T$ )  $\leftarrow$   
initially( $F = V$ ),  
not broken( $F = V, \theta, T$ ).
```

```
holdsAt( $F = V, T$ )  $\leftarrow$   
initiatedAt( $F = V, T_s$ ),  $T_s < T$ ,  
not broken( $F = V, T_s, T$ ).  
⋮
```

# Online Probabilistic Event Calculus

## Application-Specific Rules

```
initiatedAt(moving(P1, P2) = true, T) ←  
  happensAt(walking(P1), T),  
  happensAt(walking(P2), T),  
  holdsAt(close(P1, P2) = true, T),  
  holdsAt(similarOrientation(P1, P2) = true, T).
```

```
terminatedAt(moving(P1, P2) = true, T) ←  
  happensAt(walking(P2), T),  
  holdsAt(close(P1, P2) = false, T).  
  :
```

## Event Calculus Axioms

```
holdsAt(F = V, T) ←  
  initially(F = V),  
  not broken(F = V, 0, T).
```

```
holdsAt(F = V, T) ←  
  initiatedAt(F = V, Ts), Ts < T,  
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  :
```

Prob-EC =  
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    :  
:
```

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    :  
:
```

Prob-EC =  
Event Calculus  
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## Data Stream

```
0.73 :: happensAt(walking(id0), T1)  
0.79 :: happensAt(walking(id1), T1)  
0.92 :: happensAt(active(id5), T1)  
:  
:
```

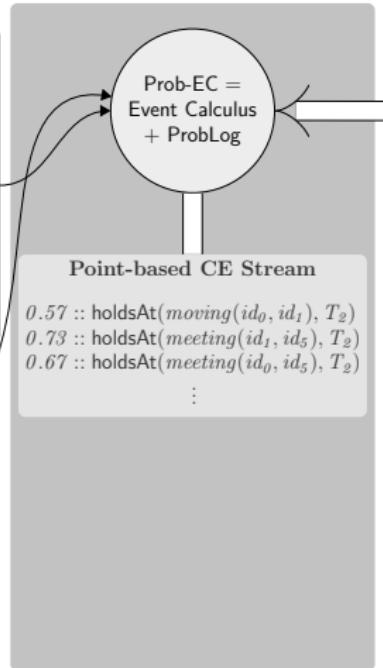
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    not broken(F = V, Ts, T).  
    :  
    :
```



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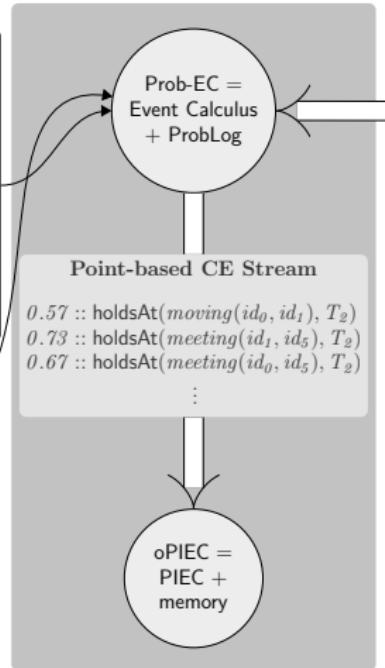
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initiatedAt(moving(P1, P2) = true, T) ←  
    happensAt(walking(P1), T),  
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terminatedAt(moving(P1, P2) = true, T) ←  
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    :
```

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    :
```



## Data Stream

```
0.73 :: happensAt(walking(id0), T1)  
0.79 :: happensAt(walking(id1), T1)  
0.92 :: happensAt(active(id5), T1)  
    :
```

## Point-based CE Stream

```
0.57 :: holdsAt(moving(id0, id1), T2)  
0.73 :: holdsAt(meeting(id1, id5), T2)  
0.67 :: holdsAt(meeting(id0, id5), T2)  
    :
```

## oPIEC = PIEC + memory

# Online Probabilistic Event Calculus

## Application-Specific Rules

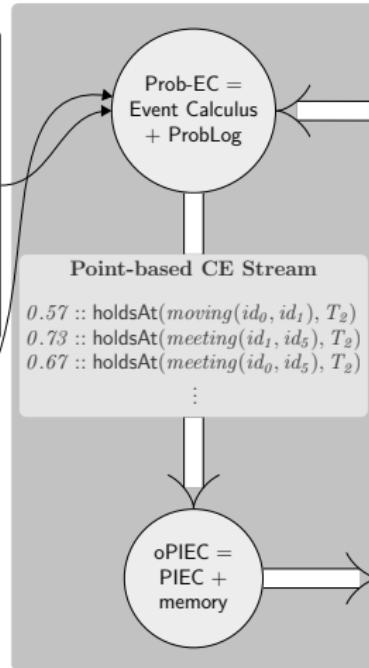
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    happensAt(walking(P1), T),  
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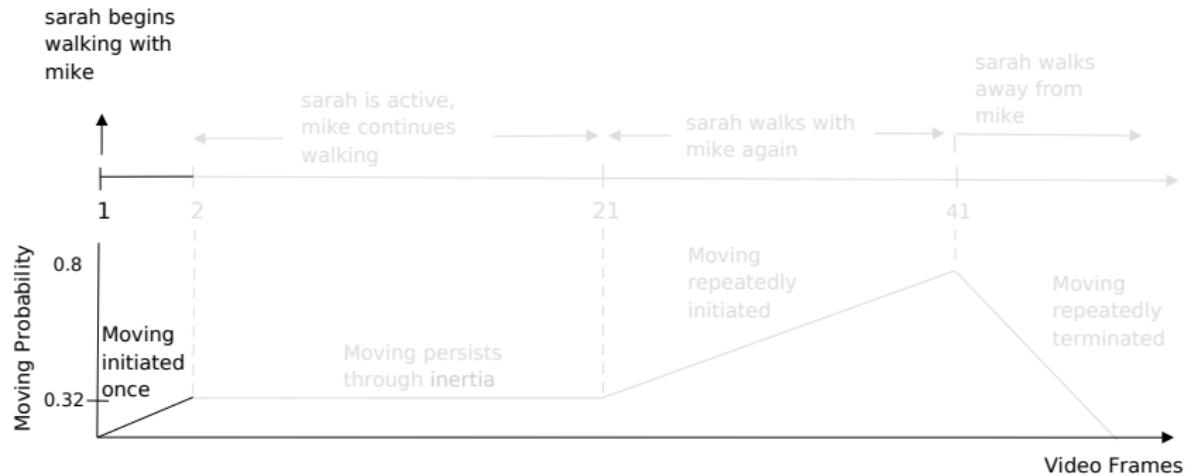
## Data Stream

```
0.73 :: happensAt(walking(id0), T1)  
0.79 :: happensAt(walking(id1), T1)  
0.92 :: happensAt(active(id5), T1)  
⋮
```

## Interval-based CE Stream

```
0.61 :: holdsFor(moving(id0, id1), (T2, T5))  
0.88 :: holdsFor(meeting(id1, id5), (T2, T4))  
0.66 :: holdsFor(meeting(id0, id5), (T2, T9))  
⋮
```

# Instantaneous Recognition

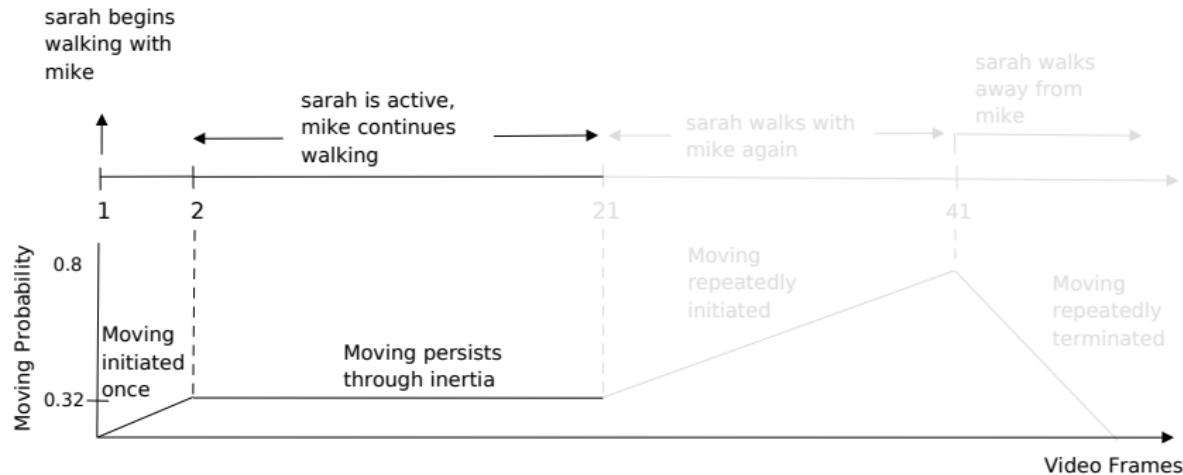


**initiatedAt**(*moving(P<sub>1</sub>, P<sub>2</sub>)*=true, *T*)  $\leftarrow$   
**happensAt**(*walking(P<sub>1</sub>)*, *T*),  
**happensAt**(*walking(P<sub>2</sub>)*, *T*),  
**holdsAt**(*close(P<sub>1</sub>, P<sub>2</sub>)*=true, *T*),  
**holdsAt**(*similarOrientation(P<sub>1</sub>, P<sub>2</sub>)*=true, *T*).

**terminatedAt**(*moving(P<sub>1</sub>, P<sub>2</sub>)*=true, *T*)  $\leftarrow$   
**happensAt**(*walking(P<sub>1</sub>)*, *T*),  
**holdsAt**(*close(P<sub>1</sub>, P<sub>2</sub>)*=false, *T*).

0.70 :: **happensAt**(*walking(mike)*, 1).  
0.46 :: **happensAt**(*walking(sarah)*, 1).

# Instantaneous Recognition



```

initiatedAt(moving(P1, P2) = true, T) ←
  happensAt(walking(P1), T),
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  holdsAt(close(P1, P2) = true, T),
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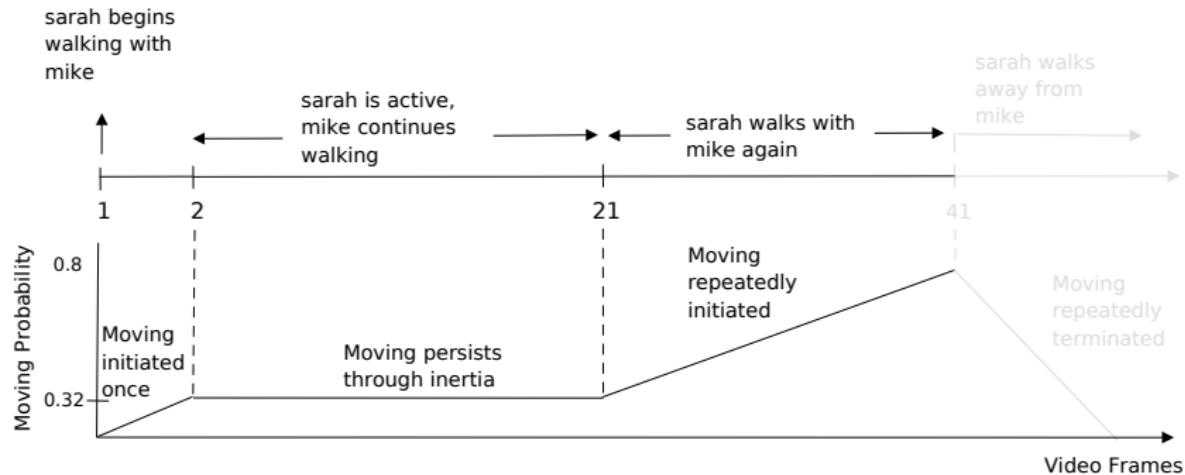
```

terminatedAt(moving(P1, P2) = true, T) ←
  happensAt(walking(P1), T),
  holdsAt(close(P1, P2) = false, T).
  
```

```

0.70 :: happensAt(walking(mike), 1).
0.46 :: happensAt(walking(sarah), 1).
0.73 :: happensAt(walking(mike), 2).
0.55 :: happensAt(active(sarah), 2). ...
  
```

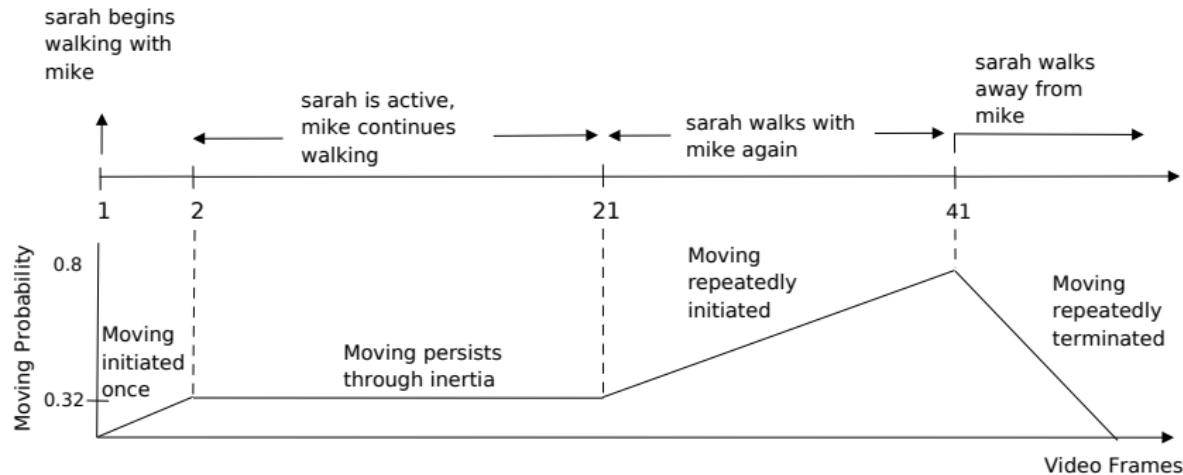
# Instantaneous Recognition



**initiatedAt( $\text{moving}(P_1, P_2) = \text{true}$ ,  $T$ ) \leftarrow**  
happensAt(walking( $P_1$ ),  $T$ ),  
happensAt(walking( $P_2$ ),  $T$ ),  
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happensAt(walking( $P_1$ ),  $T$ ),  
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0.70 :: happensAt(walking(mike), 1).  
0.46 :: happensAt(walking(sarah), 1).  
0.73 :: happensAt(walking(mike), 2).  
0.55 :: happensAt(active(sarah), 2). ...  
0.69 :: happensAt(walking(mike), 21).  
0.58 :: happensAt(walking(sarah), 21). ...

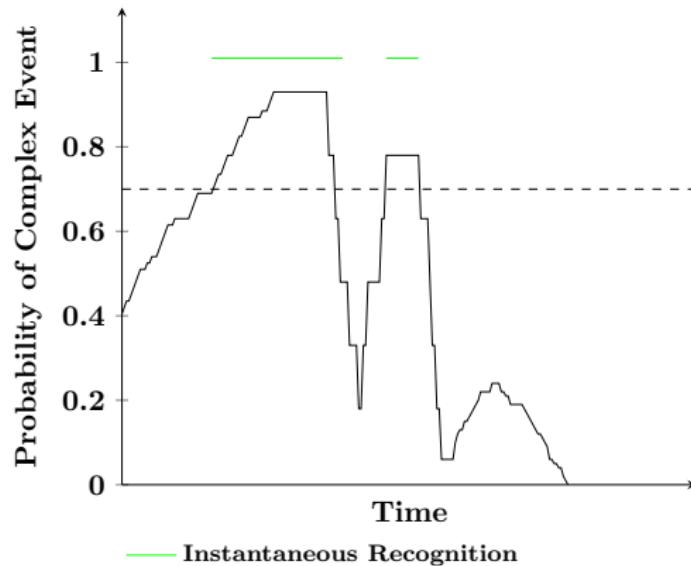
# Instantaneous Recognition



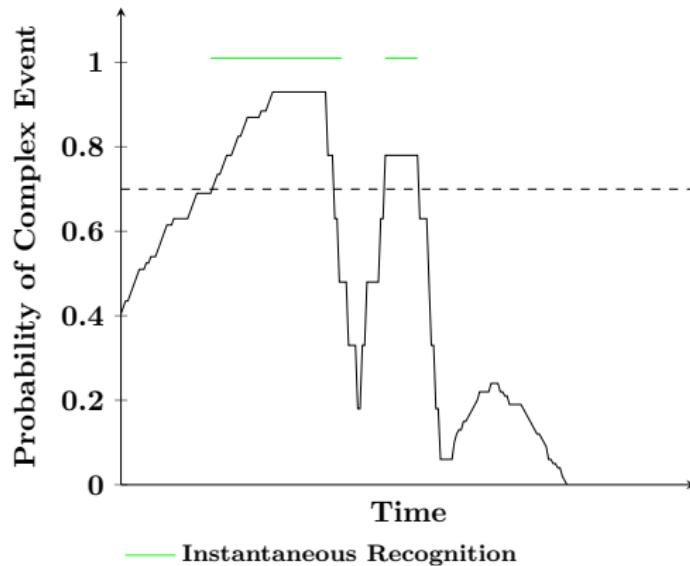
**initiatedAt**( $\text{moving}(P_1, P_2) = \text{true}$ ,  $T$ )  $\leftarrow$   
**happensAt**( $\text{walking}(P_1)$ ,  $T$ ),  
**happensAt**( $\text{walking}(P_2)$ ,  $T$ ),  
**holdsAt**( $\text{close}(P_1, P_2) = \text{true}$ ,  $T$ ),  
**holdsAt**( $\text{similarOrientation}(P_1, P_2) = \text{true}$ ,  $T$ ).  
**terminatedAt**( $\text{moving}(P_1, P_2) = \text{true}$ ,  $T$ )  $\leftarrow$   
**happensAt**( $\text{walking}(P_1)$ ,  $T$ ),  
**holdsAt**( $\text{close}(P_1, P_2) = \text{false}$ ,  $T$ ).

0.70 :: **happensAt**( $\text{walking}(mike)$ , 1).  
0.46 :: **happensAt**( $\text{walking}(sarah)$ , 1).  
0.73 :: **happensAt**( $\text{walking}(mike)$ , 2).  
0.55 :: **happensAt**( $\text{active}(sarah)$ , 2). ...  
0.69 :: **happensAt**( $\text{walking}(mike)$ , 21).  
0.58 :: **happensAt**( $\text{walking}(sarah)$ , 21). ...  
0.82 :: **happensAt**( $\text{inactive}(mike)$ , 41).  
0.79 :: **happensAt**( $\text{walking}(sarah)$ , 41). ...

# Instantaneous Recognition



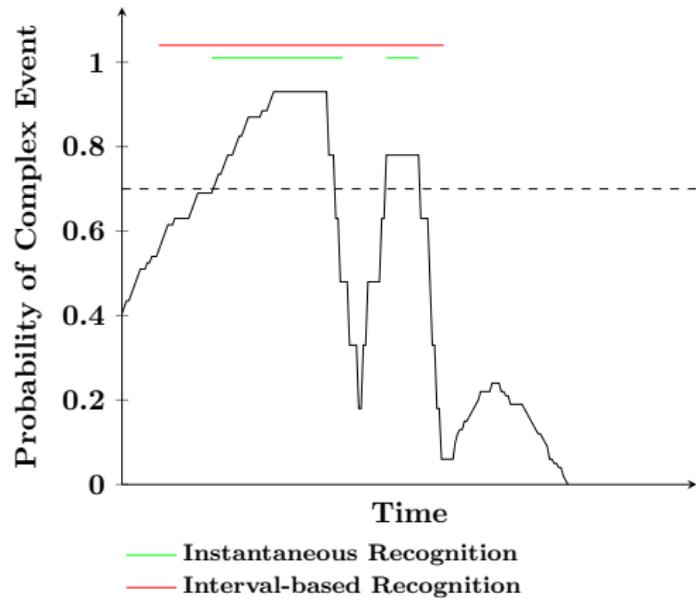
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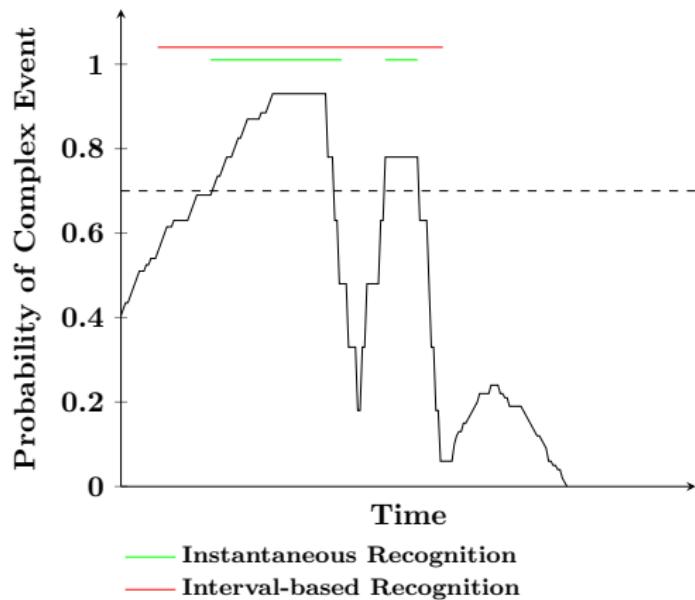
Higher accuracy than crisp reasoning in the presence of:

- several initiations and terminations;
- few probabilistic conjuncts.

# Instantaneous vs Interval-based Recognition

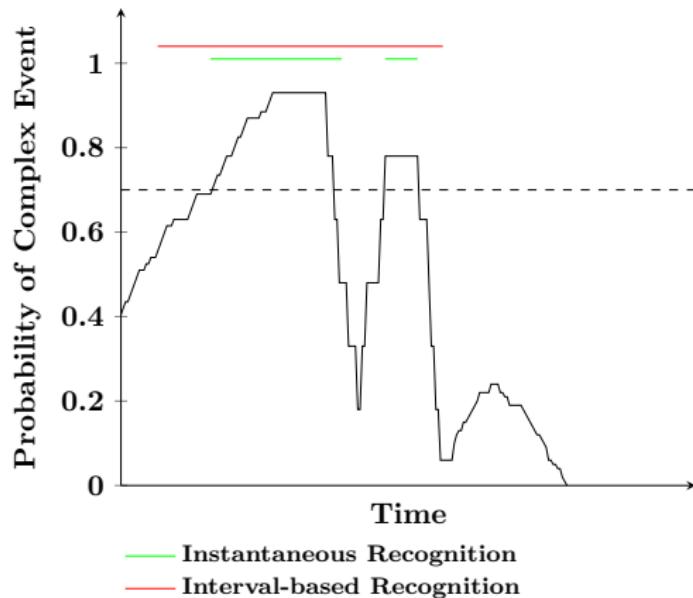


# Instantaneous vs Interval-based Recognition



- **Interval Probability:** average probability of the time-points it contains.

# Instantaneous vs Interval-based Recognition



- **Interval Probability:** average probability of the time-points it contains.
- **Probabilistic Maximal Interval:**
  - probability above a given threshold;
  - no super-interval with probability above the threshold.

## Interval-based Recognition

Time	1	2	3	4	5	6	7	8	9	10
<i>In</i>	0	0.5	0.7	0.9	0.4	0.1	0	0	0.5	1

## Interval-based Recognition

Time	1	2	3	4	5	6	7	8	9	10
$In$	0	0.5	0.7	0.9	0.4	0.1	0	0	0.5	1
$L$	-0.5	0	0.2	0.4	-0.1	-0.4	-0.5	-0.5	0	0.5

## Interval-based Recognition

Time	1	2	3	4	5	6	7	8	9	10
$In$	0	0.5	0.7	0.9	0.4	0.1	0	0	0.5	1
$L$	-0.5	0	0.2	0.4	-0.1	-0.4	-0.5	-0.5	0	0.5

$$\sum_{i=s}^e L[i] \geq 0 \Leftrightarrow P([s, e]) \geq \mathcal{T}$$

## Interval-based Recognition

Time	1	2	3	4	5	6	7	8	9	10
$ln$	0	0.5	0.7	0.9	0.4	0.1	0	0	0.5	1
$L$	-0.5	0	0.2	0.4	-0.1	-0.4	-0.5	-0.5	0	0.5
$prefix$	-0.5	-0.5	-0.3	0.1	0	-0.4	-0.9	-1.4	-1.4	-0.9

## Interval-based Recognition

Time	1	2	3	4	5	6	7	8	9	10
$ln$	0	0.5	0.7	0.9	0.4	0.1	0	0	0.5	1
$L$	-0.5	0	0.2	0.4	-0.1	-0.4	-0.5	-0.5	0	0.5
$prefix$	-0.5	-0.5	-0.3	0.1	0	-0.4	-0.9	-1.4	-1.4	-0.9
$dp$										-0.9

## Interval-based Recognition

Time	1	2	3	4	5	6	7	8	9	10
$ln$	0	0.5	0.7	0.9	0.4	0.1	0	0	0.5	1
$L$	-0.5	0	0.2	0.4	-0.1	-0.4	-0.5	-0.5	0	0.5
$prefix$	-0.5	-0.5	-0.3	0.1	0	-0.4	-0.9	-1.4	-1.4	-0.9
$dp$									-0.9	-0.9

## Interval-based Recognition

Time	1	2	3	4	5	6	7	8	9	10
$ln$	0	0.5	0.7	0.9	0.4	0.1	0	0	0.5	1
$L$	-0.5	0	0.2	0.4	-0.1	-0.4	-0.5	-0.5	0	0.5
$prefix$	-0.5	-0.5	-0.3	0.1	0	-0.4	-0.9	-1.4	-1.4	-0.9
$dp$								-0.9	-0.9	-0.9

## Interval-based Recognition

Time	1	2	3	4	5	6	7	8	9	10
$ln$	0	0.5	0.7	0.9	0.4	0.1	0	0	0.5	1
$L$	-0.5	0	0.2	0.4	-0.1	-0.4	-0.5	-0.5	0	0.5
$prefix$	-0.5	-0.5	-0.3	0.1	0	-0.4	-0.9	-1.4	-1.4	-0.9
$dp$							-0.9	-0.9	-0.9	-0.9

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Time	1	2	3	4	5	6	7	8	9	10
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$prefix$	-0.5	-0.5	-0.3	0.1	0	-0.4	-0.9	-1.4	-1.4	-0.9
$dp$						-0.4	-0.9	-0.9	-0.9	-0.9

## Interval-based Recognition

Time	1	2	3	4	5	6	7	8	9	10
$ln$	0	0.5	0.7	0.9	0.4	0.1	0	0	0.5	1
$L$	-0.5	0	0.2	0.4	-0.1	-0.4	-0.5	-0.5	0	0.5
$prefix$	-0.5	-0.5	-0.3	0.1	0	-0.4	-0.9	-1.4	-1.4	-0.9
$dp$	0.1	0.1	0.1	0.1	0	-0.4	-0.9	-0.9	-0.9	-0.9

## Interval-based Recognition

Time	1	2	3	4	5	6	7	8	9	10
$ln$	0	0.5	0.7	0.9	0.4	0.1	0	0	0.5	1
$L$	-0.5	0	0.2	0.4	-0.1	-0.4	-0.5	-0.5	0	0.5
$prefix$	-0.5	-0.5	-0.3	0.1	0	-0.4	-0.9	-1.4	-1.4	-0.9
$dp$	0.1	0.1	0.1	0.1	0	-0.4	-0.9	-0.9	-0.9	-0.9

$$dprange[s, e] = \begin{cases} dp[e] - prefix[s-1] & \text{if } s > 1 \\ dp[e] & \text{if } s = 1 \end{cases}$$

## Interval-based Recognition

Time	1	2	3	4	5	6	7	8	9	10
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$L$	-0.5	0	0.2	0.4	-0.1	-0.4	-0.5	-0.5	0	0.5
$prefix$	-0.5	-0.5	-0.3	0.1	0	-0.4	-0.9	-1.4	-1.4	-0.9
$dp$	0.1	0.1	0.1	0.1	0	-0.4	-0.9	-0.9	-0.9	-0.9

$$dprange[s, e] = \begin{cases} dp[e] - prefix[s-1] & \text{if } s > 1 \\ dp[e] & \text{if } s = 1 \end{cases}$$

$$dprange[s, e] \geq 0 \Rightarrow \exists e^* : e^* \geq e, P([s, e^*] \geq T)$$

## Interval-based Recognition

Time	1	2	3	4	5	6	7	8	9	10
$In$	0	0.5	0.7	0.9	0.4	0.1	0	0	0.5	1
$L$	-0.5	0	0.2	0.4	-0.1	-0.4	-0.5	-0.5	0	0.5
$prefix$	-0.5	-0.5	-0.3	0.1	0	-0.4	-0.9	-1.4	-1.4	-0.9
$dp$	0.1	0.1	0.1	0.1	0	-0.4	-0.9	-0.9	-0.9	-0.9

## Interval-based Recognition

Time	1	2	3	4	5	6	7	8	9	10
$ln$	0	0.5	0.7	0.9	0.4	0.1	0	0	0.5	1
$L$	-0.5	0	0.2	0.4	-0.1	-0.4	-0.5	-0.5	0	0.5
$prefix$	-0.5	-0.5	-0.3	0.1	0	-0.4	-0.9	-1.4	-1.4	-0.9
$dp$	0.1	0.1	0.1	0.1	0	-0.4	-0.9	-0.9	-0.9	-0.9

$$dprange[1, 1] = dp[1] = 0.1 \geq 0$$

## Interval-based Recognition

Time	↑	↓								
	1	2	3	4	5	6	7	8	9	10
$ln$	0	0.5	0.7	0.9	0.4	0.1	0	0	0.5	1
$L$	-0.5	0	0.2	0.4	-0.1	-0.4	-0.5	-0.5	0	0.5
$prefix$	-0.5	-0.5	-0.3	0.1	0	-0.4	-0.9	-1.4	-1.4	-0.9
$dp$	0.1	0.1	0.1	0.1	0	-0.4	-0.9	-0.9	-0.9	-0.9

## Interval-based Recognition

Time	↑	↓								
	1	2	3	4	5	6	7	8	9	10
$ln$	0	0.5	0.7	0.9	0.4	0.1	0	0	0.5	1
$L$	-0.5	0	0.2	0.4	-0.1	-0.4	-0.5	-0.5	0	0.5
$prefix$	-0.5	-0.5	-0.3	0.1	0	-0.4	-0.9	-1.4	-1.4	-0.9
$dp$	0.1	0.1	0.1	0.1	0	-0.4	-0.9	-0.9	-0.9	-0.9

$$dprange[1, 2] = dp[2] = 0.1 \geq 0$$

## Interval-based Recognition

Time												
	↑	↓	1	2	3	4	5	6	7	8	9	10
$ln$	0	0.5	0.7	0.9	0.4	0.1	0	0	0	0.5	1	
$L$	-0.5	0	0.2	0.4	-0.1	-0.4	-0.5	-0.5	0	0.5		
$prefix$	-0.5	-0.5	-0.3	0.1	0	-0.4	-0.9	-1.4	-1.4	-0.9	-0.9	
$dp$	0.1	0.1	0.1	0.1	0	-0.4	-0.9	-0.9	-0.9	-0.9	-0.9	

$$dprange[1, 3] = dp[3] = 0.1 \geq 0$$

## Interval-based Recognition

Time	↑				↓					
	1	2	3	4	5	6	7	8	9	10
$ln$	0	0.5	0.7	0.9	0.4	0.1	0	0	0.5	1
$L$	-0.5	0	0.2	0.4	-0.1	-0.4	-0.5	-0.5	0	0.5
$prefix$	-0.5	-0.5	-0.3	0.1	0	-0.4	-0.9	-1.4	-1.4	-0.9
$dp$	0.1	0.1	0.1	0.1	0	-0.4	-0.9	-0.9	-0.9	-0.9

$$dprange[1, 4] = dp[4] = 0.1 \geq 0$$

## Interval-based Recognition

Time	↑					↓				
	1	2	3	4	5	6	7	8	9	10
$ln$	0	0.5	0.7	0.9	0.4	0.1	0	0	0.5	1
$L$	-0.5	0	0.2	0.4	-0.1	-0.4	-0.5	-0.5	0	0.5
$prefix$	-0.5	-0.5	-0.3	0.1	0	-0.4	-0.9	-1.4	-1.4	-0.9
$dp$	0.1	0.1	0.1	0.1	0	-0.4	-0.9	-0.9	-0.9	-0.9

$$dprange[1, 5] = dp[5] = 0 \geq 0$$

## Interval-based Recognition

Time	↑					↓				
	1	2	3	4	5	6	7	8	9	10
$ln$	0	0.5	0.7	0.9	0.4	0.1	0	0	0.5	1
$L$	-0.5	0	0.2	0.4	-0.1	-0.4	-0.5	-0.5	0	0.5
$prefix$	-0.5	-0.5	-0.3	0.1	0	-0.4	-0.9	-1.4	-1.4	-0.9
$dp$	0.1	0.1	0.1	0.1	0	-0.4	-0.9	-0.9	-0.9	-0.9

$$dprange[1, 6] = dp[6] = -0.4 < 0$$

## Interval-based Recognition



Time	↑					↓				
	1	2	3	4	5	6	7	8	9	10
$ln$	0	0.5	0.7	0.9	0.4	0.1	0	0	0.5	1
$L$	-0.5	0	0.2	0.4	-0.1	-0.4	-0.5	-0.5	0	0.5
$prefix$	-0.5	-0.5	-0.3	0.1	0	-0.4	-0.9	-1.4	-1.4	-0.9
$dp$	0.1	0.1	0.1	0.1	0	-0.4	-0.9	-0.9	-0.9	-0.9

$$dprange[1, 6] = dp[6] = -0.4 < 0$$

## Interval-based Recognition



Time	1	2	3	4	5	6	7	8	9	10
$ln$	0	0.5	0.7	0.9	0.4	0.1	0	0	0.5	1
$L$	-0.5	0	0.2	0.4	-0.1	-0.4	-0.5	-0.5	0	0.5
$prefix$	-0.5	-0.5	-0.3	0.1	0	-0.4	-0.9	-1.4	-1.4	-0.9
$dp$	0.1	0.1	0.1	0.1	0	-0.4	-0.9	-0.9	-0.9	-0.9

$$dprange[2, 6] = dp[6] - prefix[1] = 0.1 \geq 0$$

# Interval-based Recognition



Time	1	2	3	4	5	6	7	8	9	10
$ln$	0	0.5	0.7	0.9	0.4	0.1	0	0	0.5	1
$L$	-0.5	0	0.2	0.4	-0.1	-0.4	-0.5	-0.5	0	0.5
$prefix$	-0.5	-0.5	-0.3	0.1	0	-0.4	-0.9	-1.4	-1.4	-0.9
$dp$	0.1	0.1	0.1	0.1	0	-0.4	-0.9	-0.9	-0.9	-0.9

$$dprange[2, 7] = dp[7] - prefix[1] = -0.4 < 0$$

## Interval-based Recognition



Time	1	2	3	4	5	6	7	8	9	10
$ln$	0	0.5	0.7	0.9	0.4	0.1	0	0	0.5	1
$L$	-0.5	0	0.2	0.4	-0.1	-0.4	-0.5	-0.5	0	0.5
$prefix$	-0.5	-0.5	-0.3	0.1	0	-0.4	-0.9	-1.4	-1.4	-0.9
$dp$	0.1	0.1	0.1	0.1	0	-0.4	-0.9	-0.9	-0.9	-0.9

$$dprange[2, 7] = dp[7] - prefix[1] = -0.4 < 0$$

## Interval-based Recognition



Time	1	2	3	4	5	6	7	8	9	10
$ln$	0	0.5	0.7	0.9	0.4	0.1	0	0	0.5	1
$L$	-0.5	0	0.2	0.4	-0.1	-0.4	-0.5	-0.5	0	0.5
$prefix$	-0.5	-0.5	-0.3	0.1	0	-0.4	-0.9	-1.4	-1.4	-0.9
$dp$	0.1	0.1	0.1	0.1	0	-0.4	-0.9	-0.9	-0.9	-0.9

# Interval-based Recognition



Time	1	2	3	4	5	6	7	8	9	10
$ln$	0	0.5	0.7	0.9	0.4	0.1	0	0	0.5	1
$L$	-0.5	0	0.2	0.4	-0.1	-0.4	-0.5	-0.5	0	0.5
prefix	-0.5	-0.5	-0.3	0.1	0	-0.4	-0.9	-1.4	-1.4	-0.9
$dp$	0.1	0.1	0.1	0.1	0	-0.4	-0.9	-0.9	-0.9	-0.9

## Interval Computation Correctness

An interval is computed iff it is a probabilistic maximal interval.

# Interval-based Recognition



Time	1	2	3	4	5	6	7	8	9	10
$l_n$	0	0.5	0.7	0.9	0.4	0.1	0	0	0.5	1
$L$	-0.5	0	0.2	0.4	-0.1	-0.4	-0.5	-0.5	0	0.5
prefix	-0.5	-0.5	-0.3	0.1	0	-0.4	-0.9	-1.4	-1.4	-0.9
$d_p$	0.1	0.1	0.1	0.1	0	-0.4	-0.9	-0.9	-0.9	-0.9

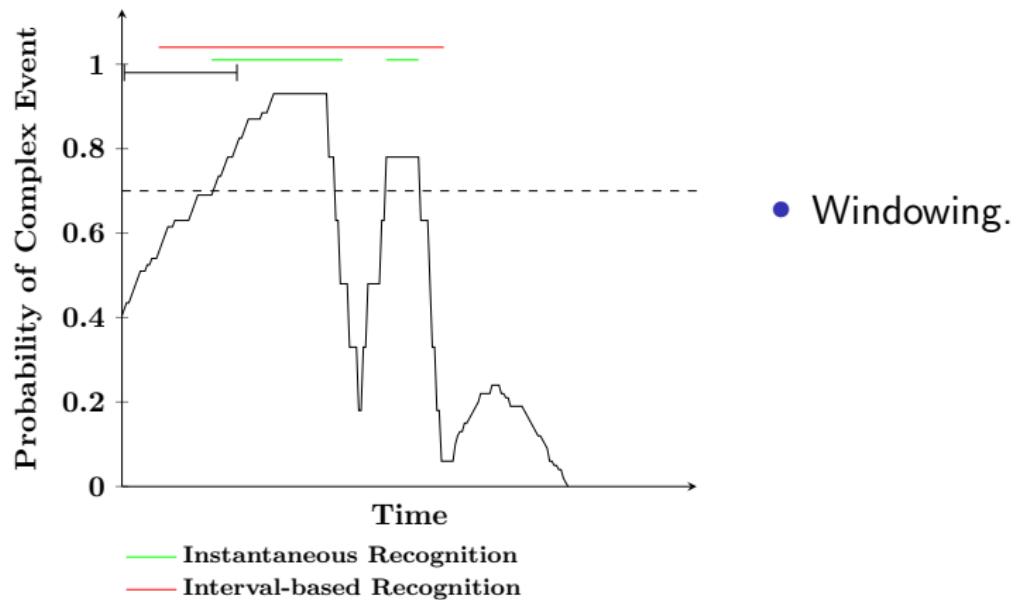
## Interval Computation Correctness

An interval is computed iff it is a probabilistic maximal interval.

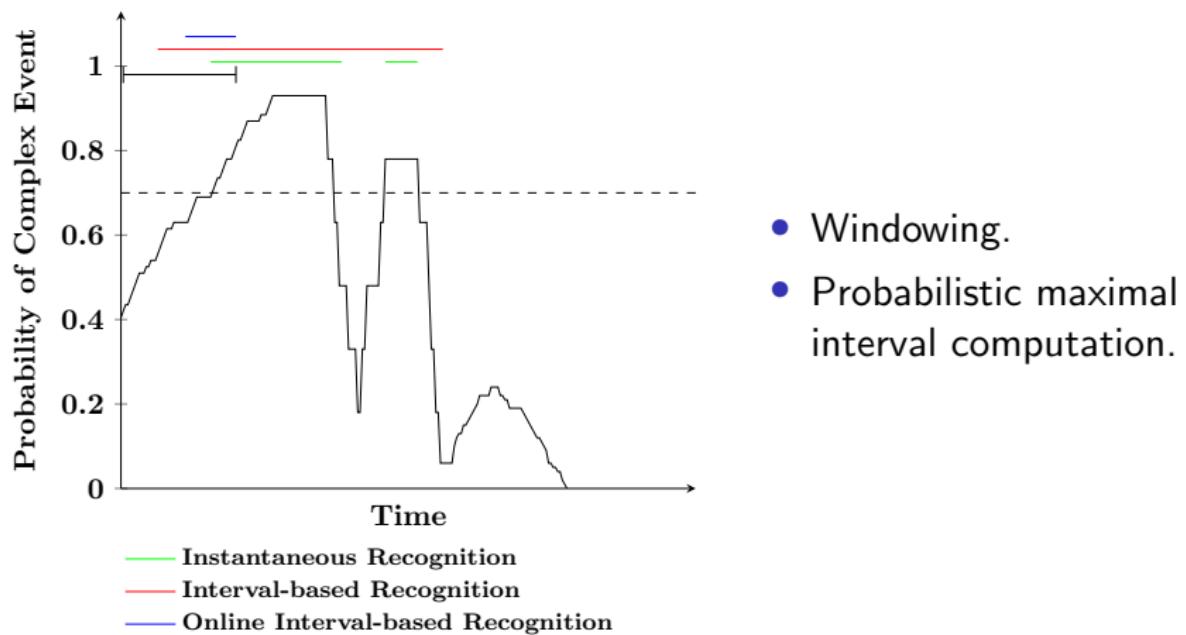
## Complexity

The computation of probabilistic maximal intervals is linear to the dataset size.

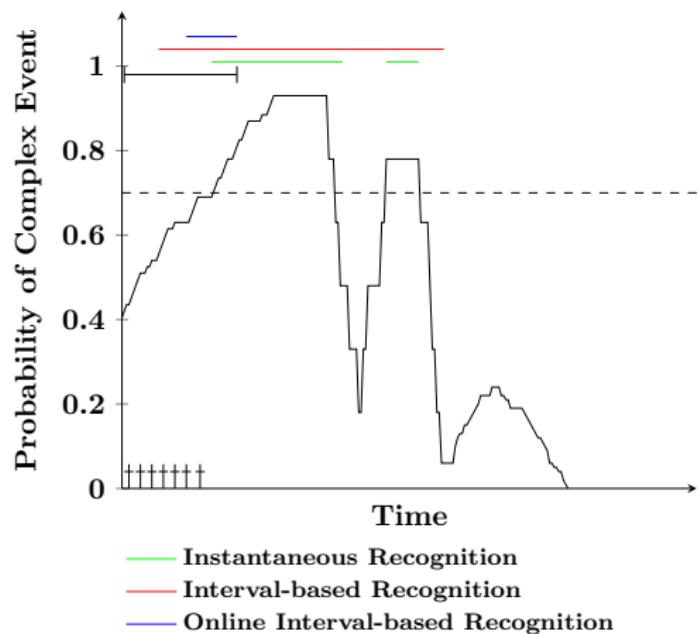
# Online Interval-based Recognition



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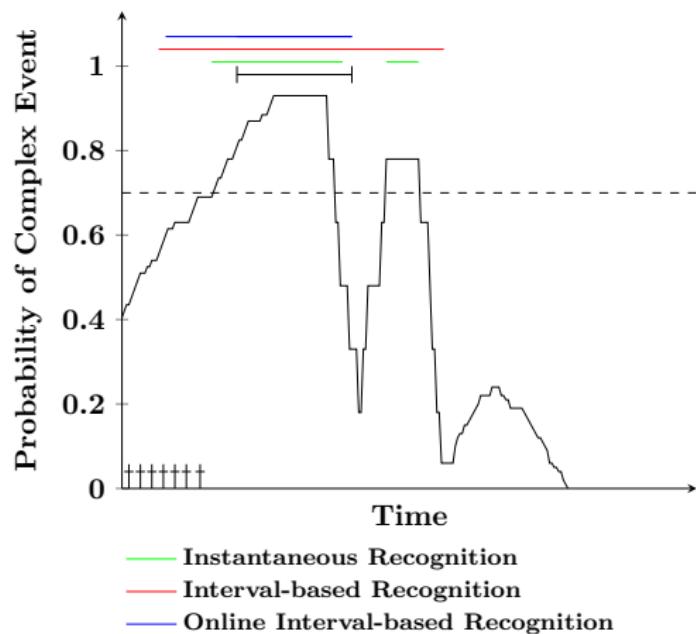


# Online Interval-based Recognition



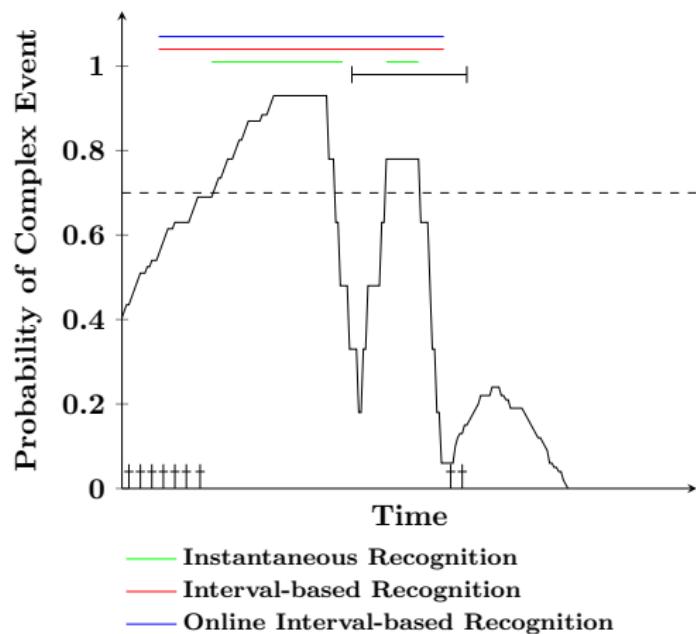
- Windowing.
- Probabilistic maximal interval computation.
- Caching potential starting points.

# Online Interval-based Recognition



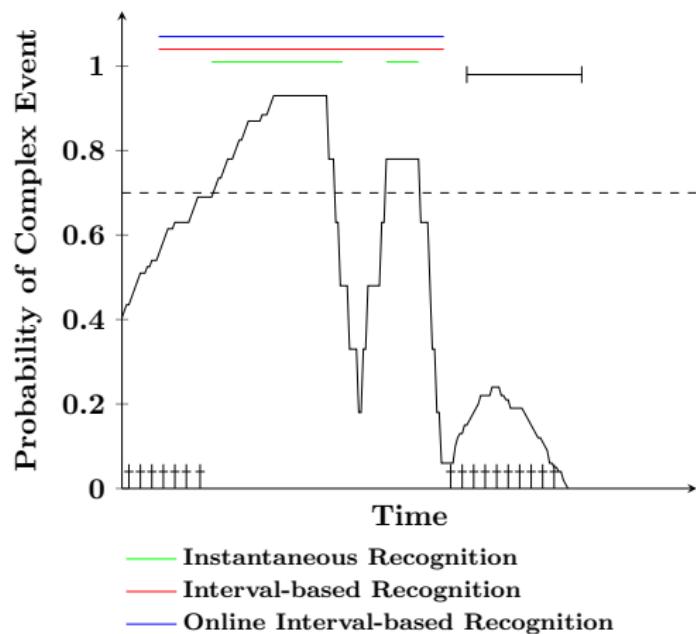
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# Online Interval-based Recognition: Properties

## Memory Minimality

A time-point is cached iff it may be the starting point of a future probabilistic maximal interval.

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An interval is computed iff it is a probabilistic maximal interval given the data seen so far.

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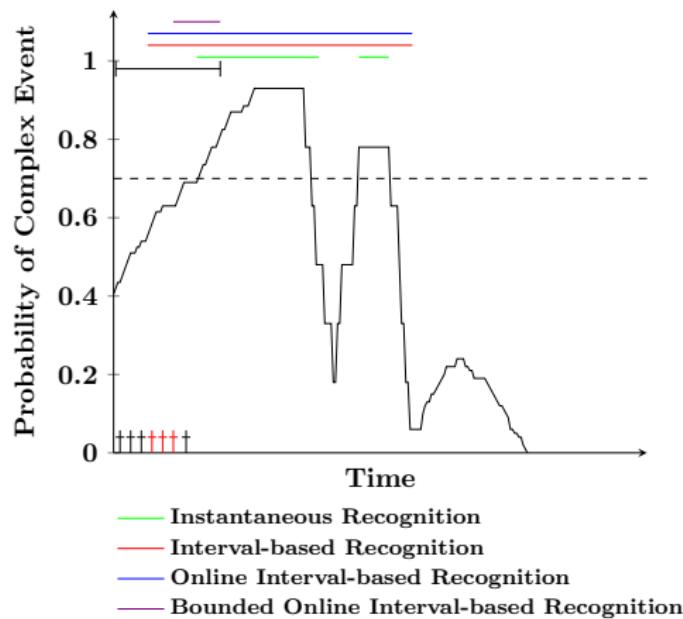
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## Complexity

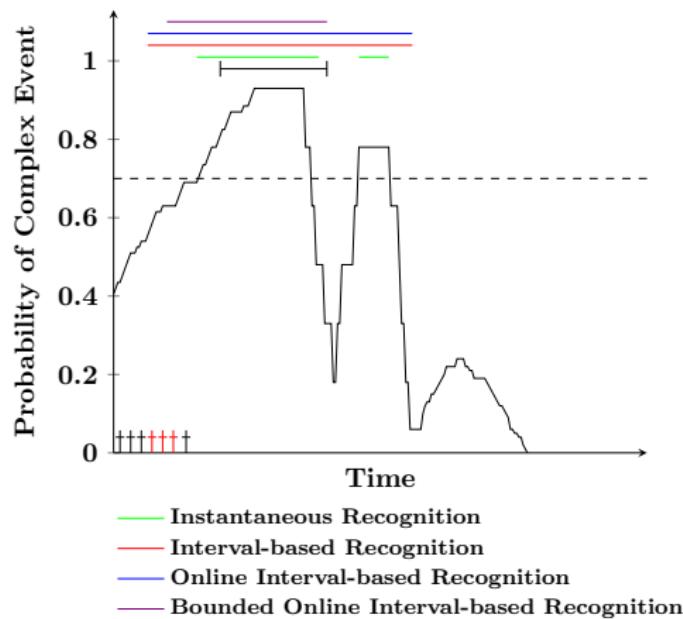
The computation of probabilistic maximal intervals is linear to the window and memory size.

# Bounded Online Interval-based Recognition



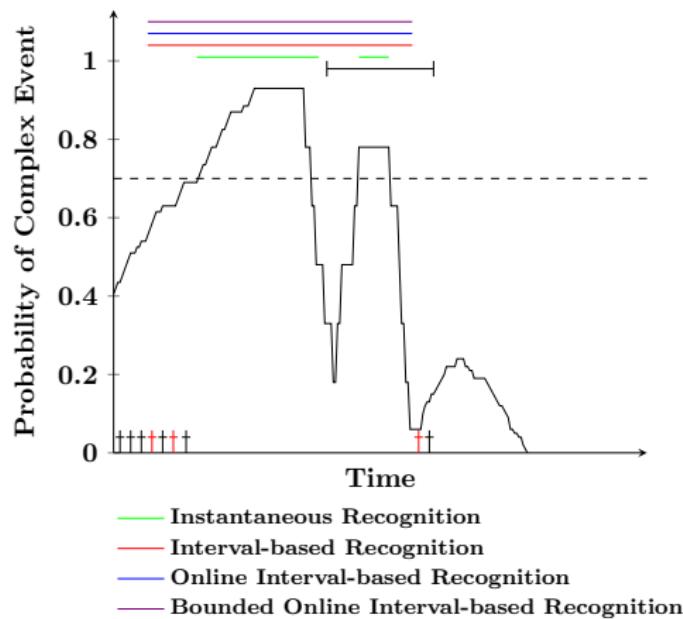
- Complex event duration statistics favor more recent potential starting points.

# Bounded Online Interval-based Recognition



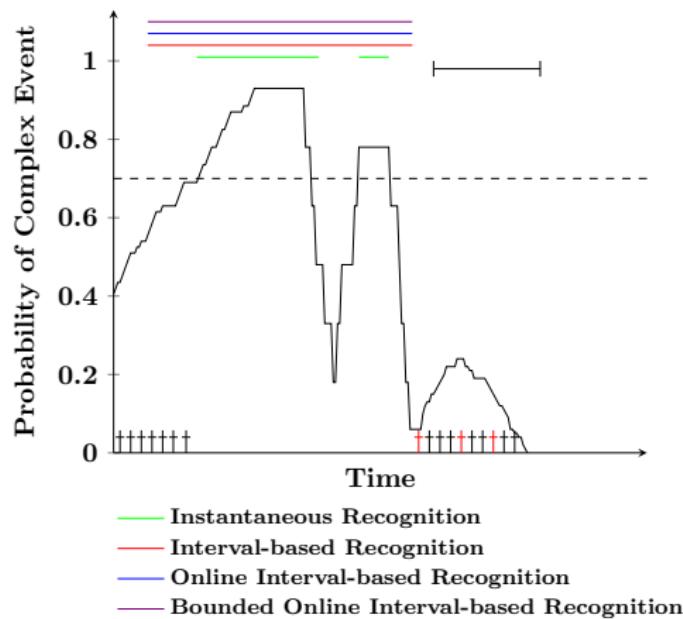
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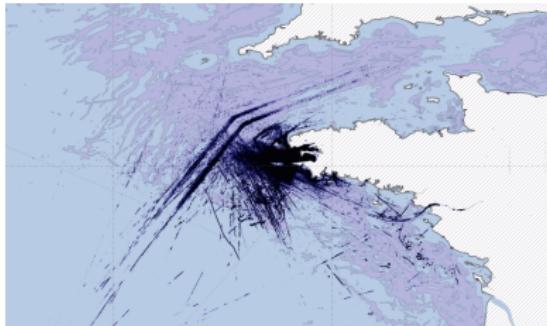
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# Bounded Online Interval-based Recognition



- Complex event duration statistics favor more recent potential starting points.
- Comparable accuracy to batch reasoning.

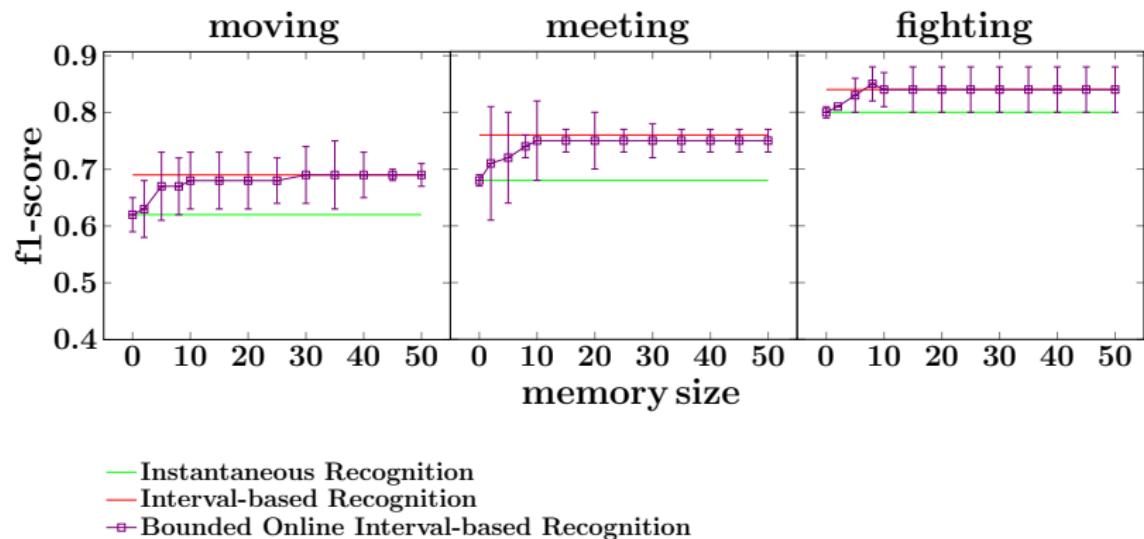
# Experimental Setup



- Human Activity Recognition:
  - Input: manually annotated simple activities on individual video frames.
  - Output: maximal intervals of complex activities.
- Maritime Situational Awareness:
  - Input: vessel position signals from the area of Brest, France.
  - Output: maximal intervals of complex vessel activities.
- <https://github.com/Periklismant/oPIEC>

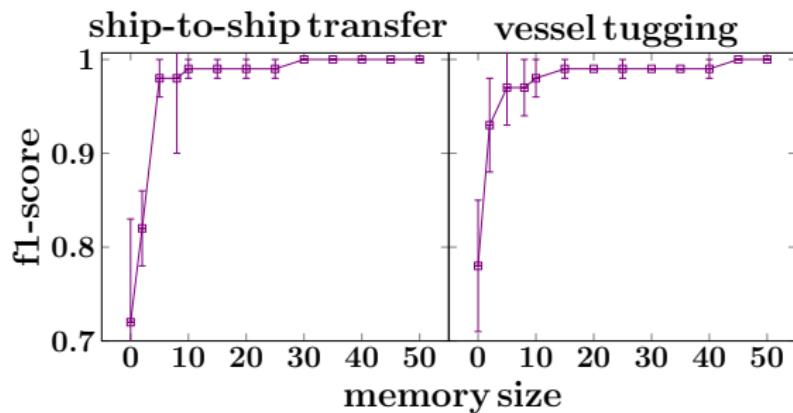
# Experimental Results: Human Activity Recognition

Comparison against ground truth



# Experimental Results: Maritime Situational Awareness

Performance of bounded online recognition against batch recognition



# Summary & Topics not Covered

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- Online reasoning over noisy streams.
- Optimal history compression for correct interval computation.
- Reproducible evaluation on benchmark, real data.

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